

# **Spatial Computing: From Manifold Geometry to Networking and Biology**

Jacob Beal

February, 2012

Work partially sponsored by DARPA; the views and conclusions contained in this document are those of the authors and not DARPA or the U.S. Government.

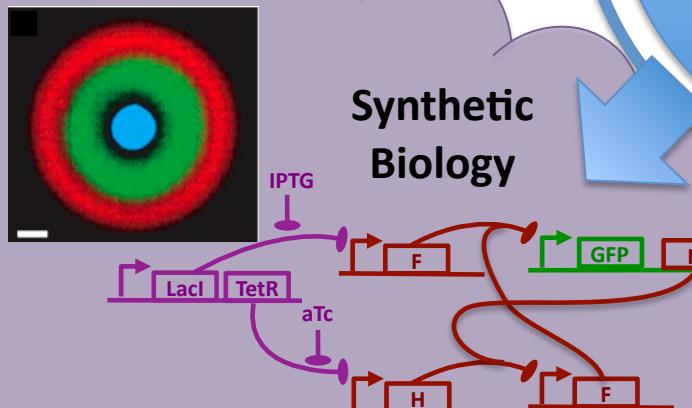
**Raytheon  
BBN Technologies**



## Distributed Power Demand Response

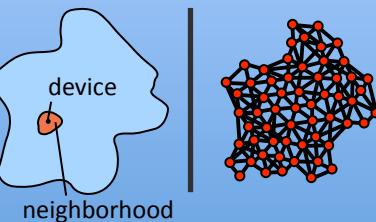
*How can millions of appliances coordinate to change how we use energy?*

*How can the parts of a design work together to adapt it to new uses?*



## Synthetic Biology

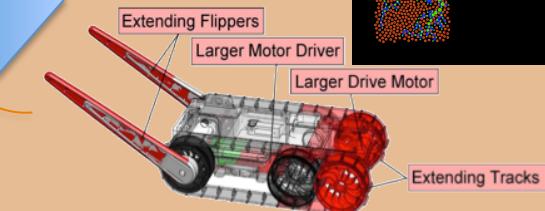
*How do you program space?*



## Spatial Computing

*How do you program the behavior of  $10^{12}$  cells?*

## Morphogenetic Engineering

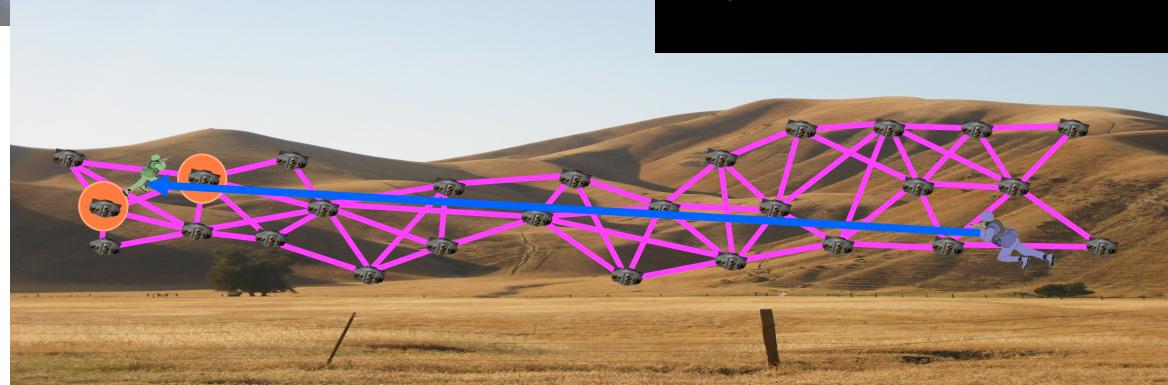
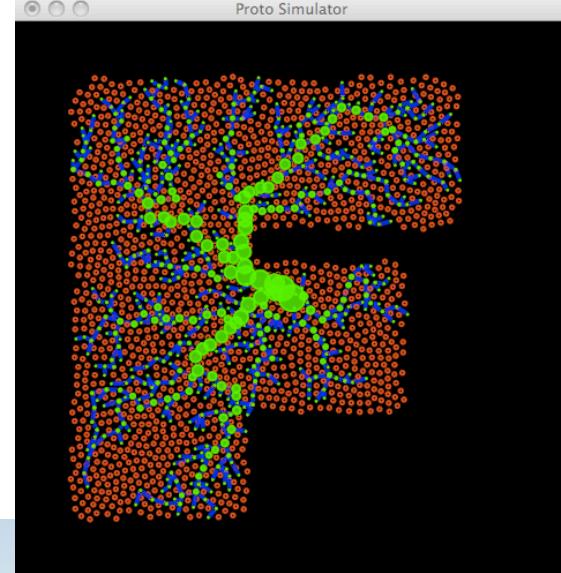


# When the world is geometric...



Pervasive Computing

Morphogenetic Engineering

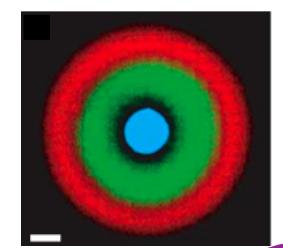
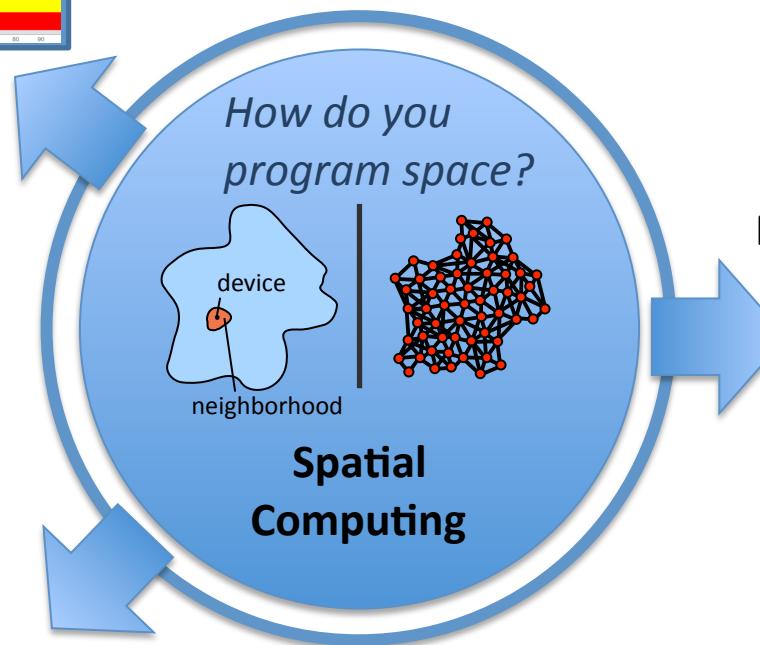


Sensor Networks

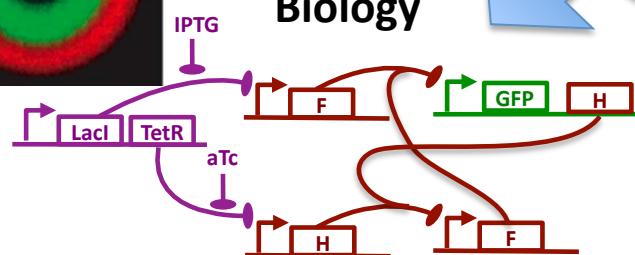
... take advantage of it!



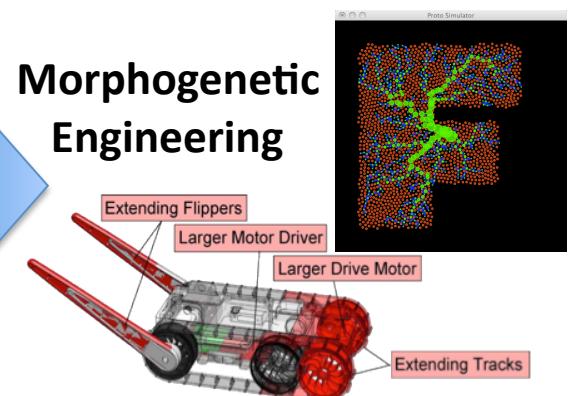
## Distributed Power Demand Response



## Synthetic Biology



## Morphogenetic Engineering



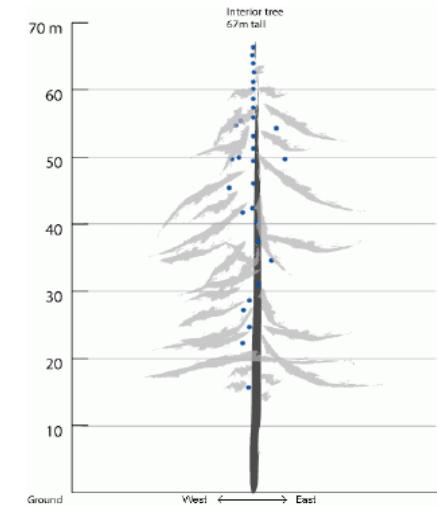
# Spatial Computers



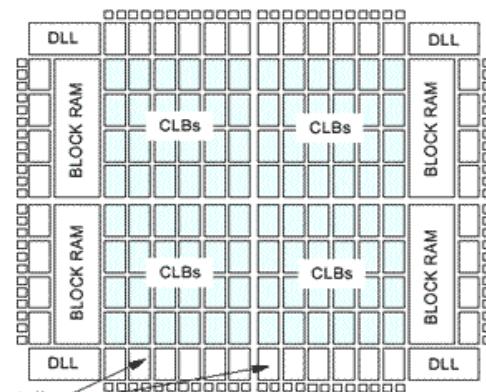
Robot Swarms



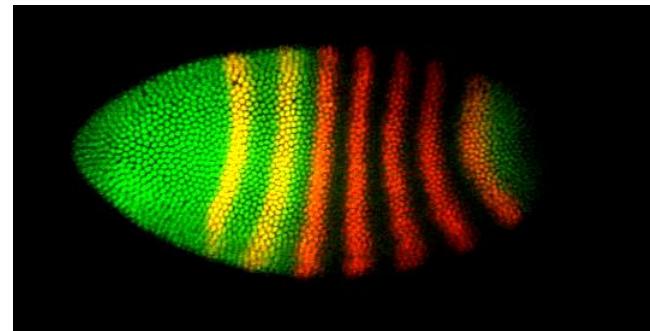
Biological Computing



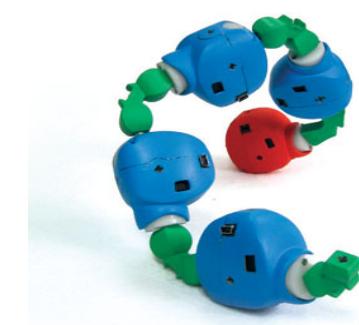
Sensor Networks



Reconfigurable Computing



Cells during Morphogenesis

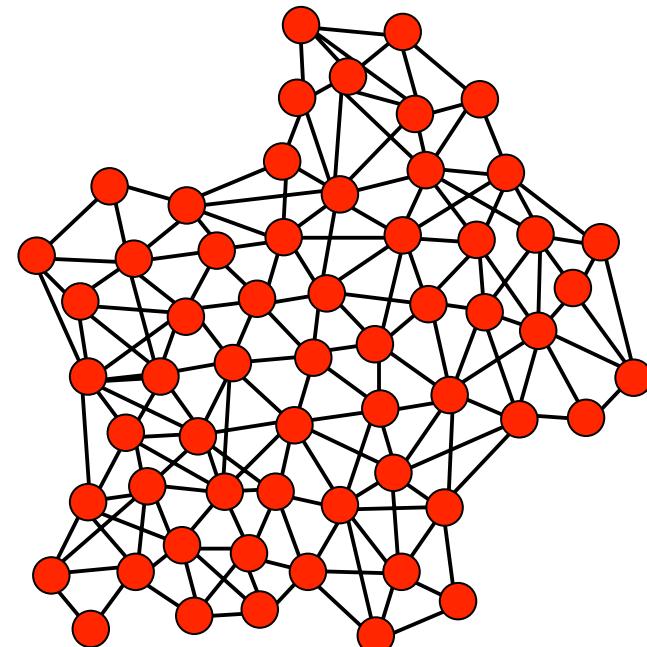
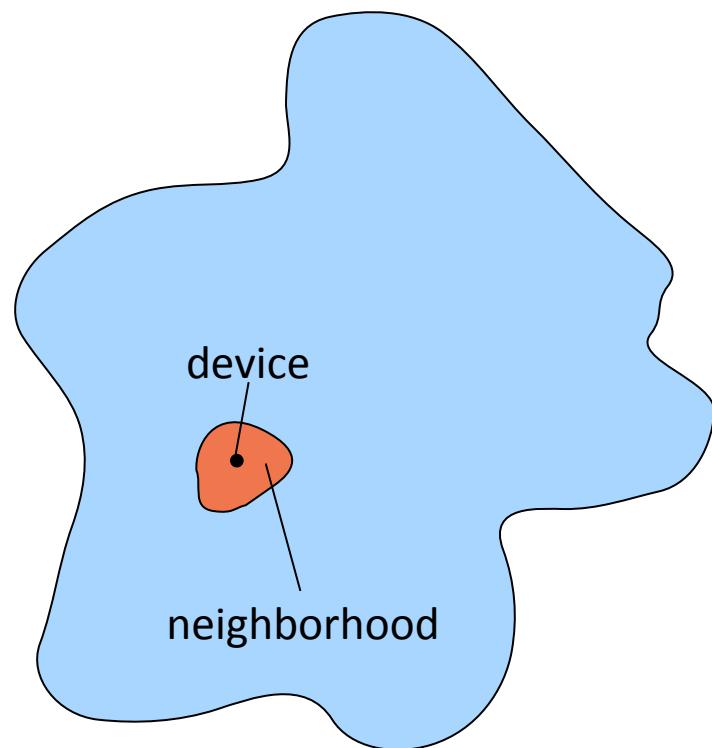


Modular Robotics

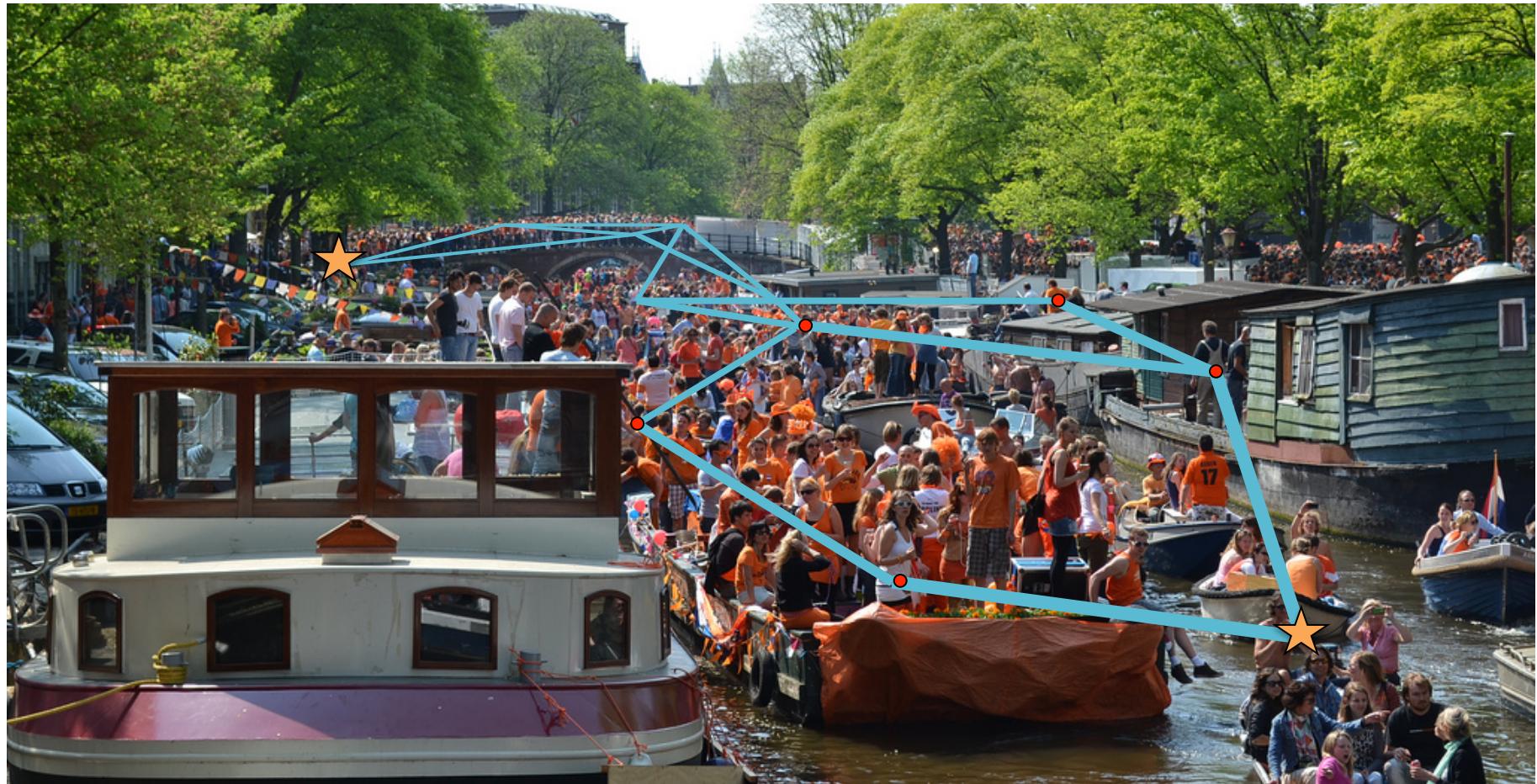
## More formally...

- A spatial computer is a collection of computational devices distributed through a physical space in which:
  - the difficulty of moving information between any two devices is strongly dependent on the distance between them, and
  - the “functional goals” of the system are generally defined in terms of the system's spatial structure

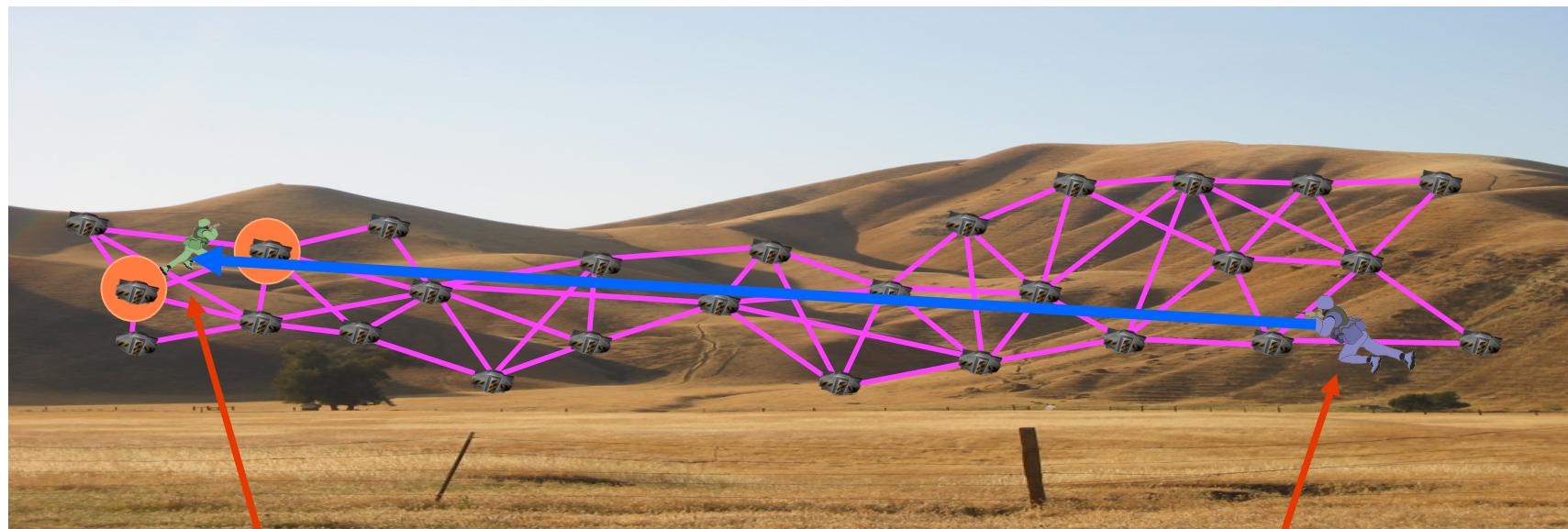
# Space/Network Duality



# Example: Mesh-Network Cell Phones



# Example: Tracking in Sensor Networks

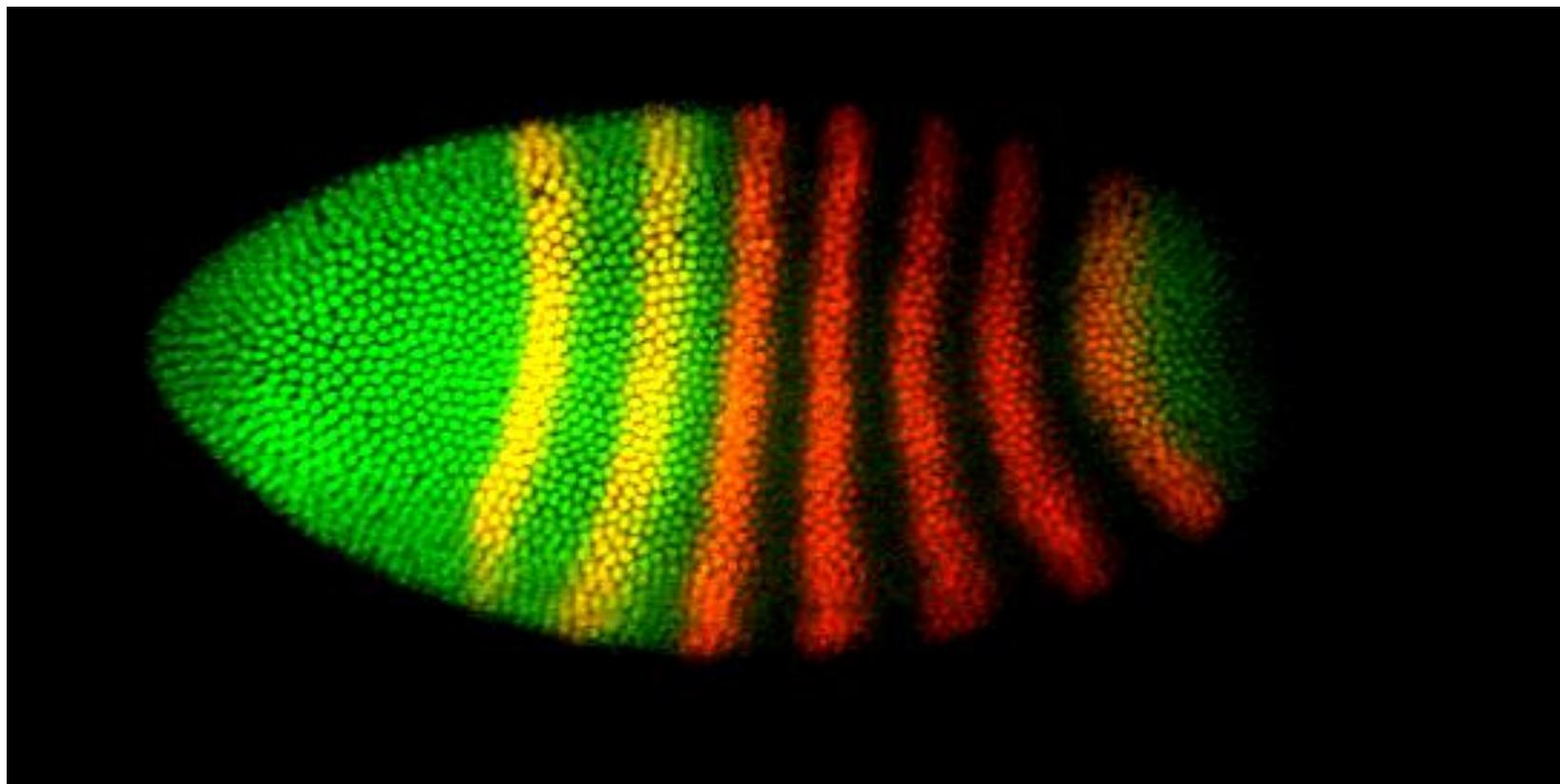


Intruder

Guard

# Example: Morphogenesis

---

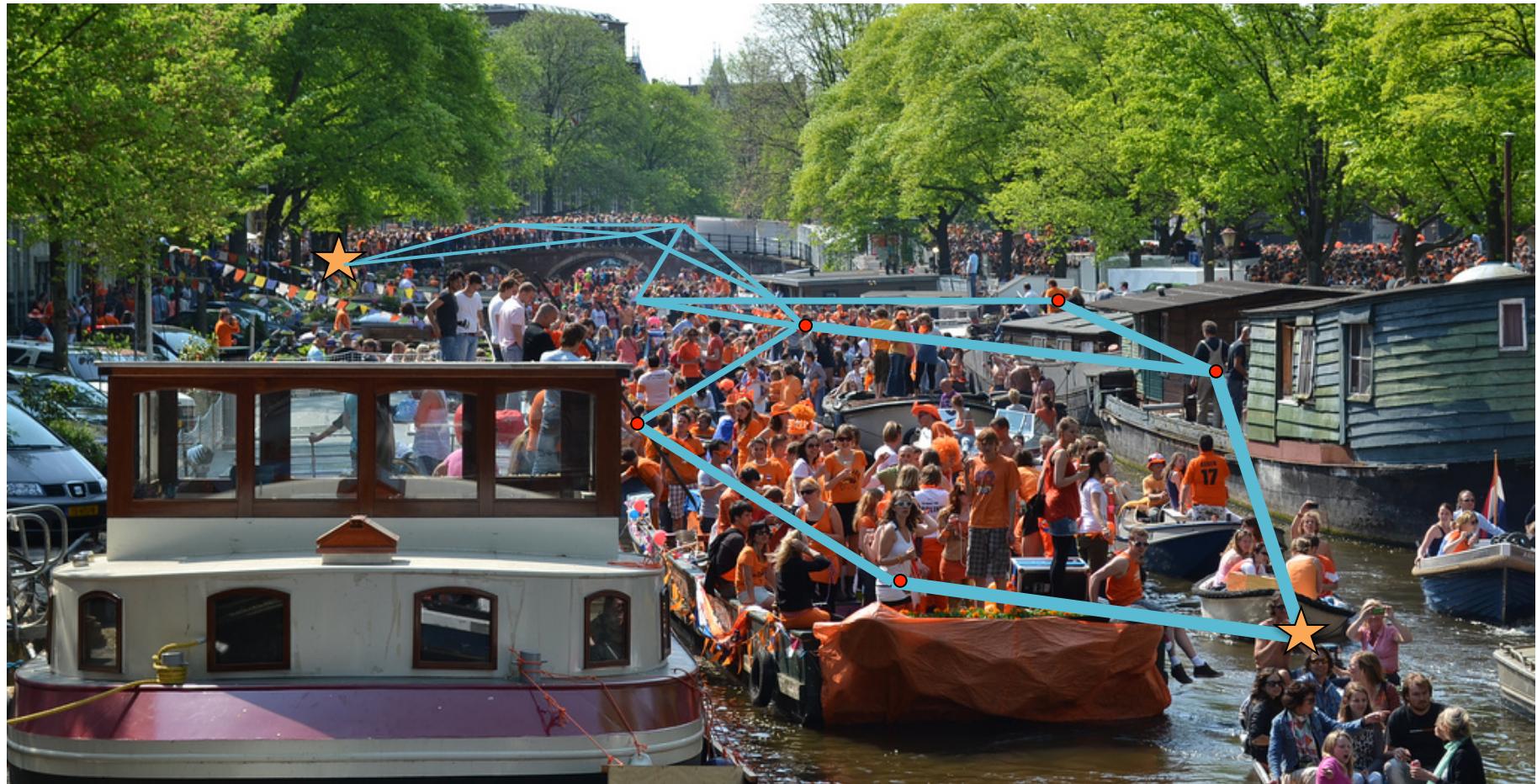


# How can we program these?

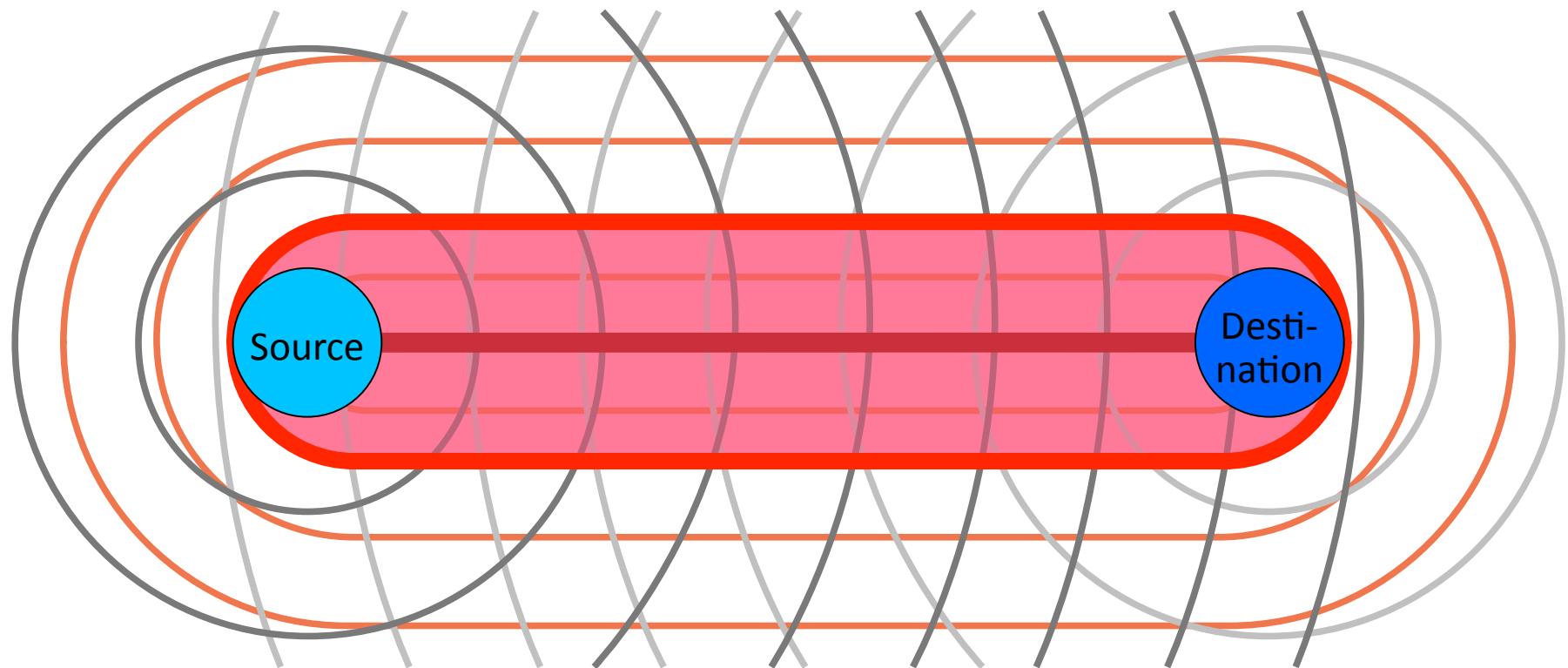
---

- Desiderata for approaches:
  - Simple, easy to understand code
  - Robust to errors, adapt to changing environment
  - Scalable to potentially vast numbers of devices
  - Take advantage of spatial nature of problems

# Example: Mesh-Network Cell Phones

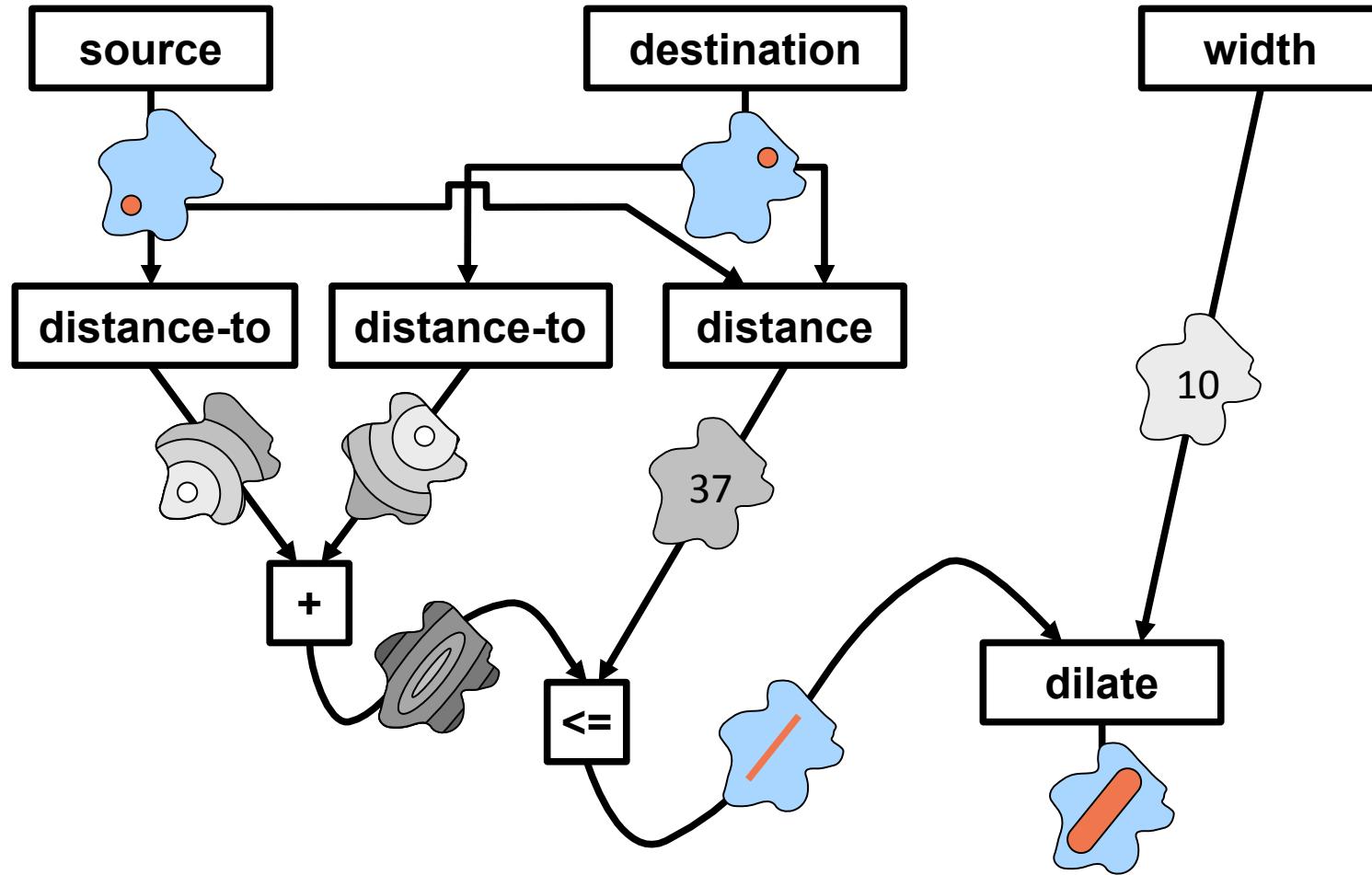


# Geometric Program: Channel

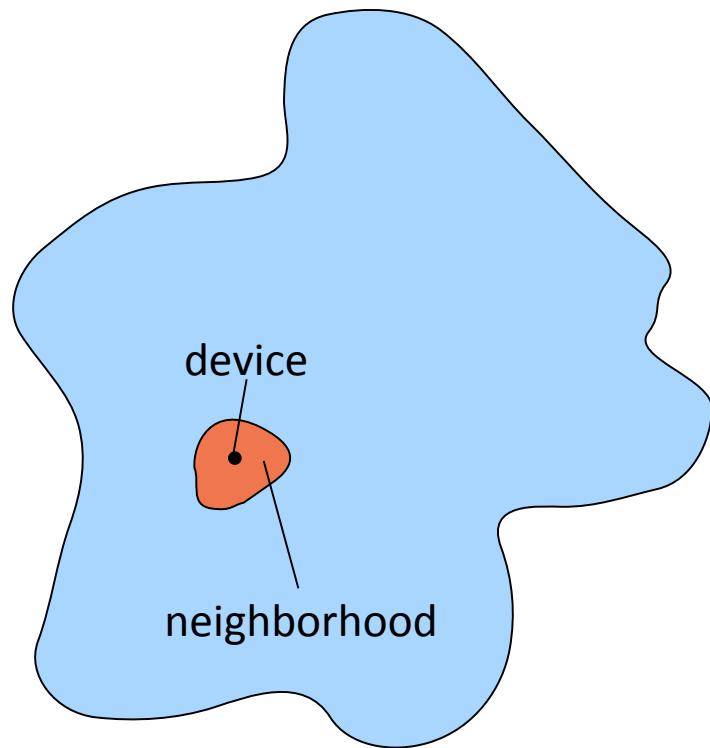


(cf. Butera)

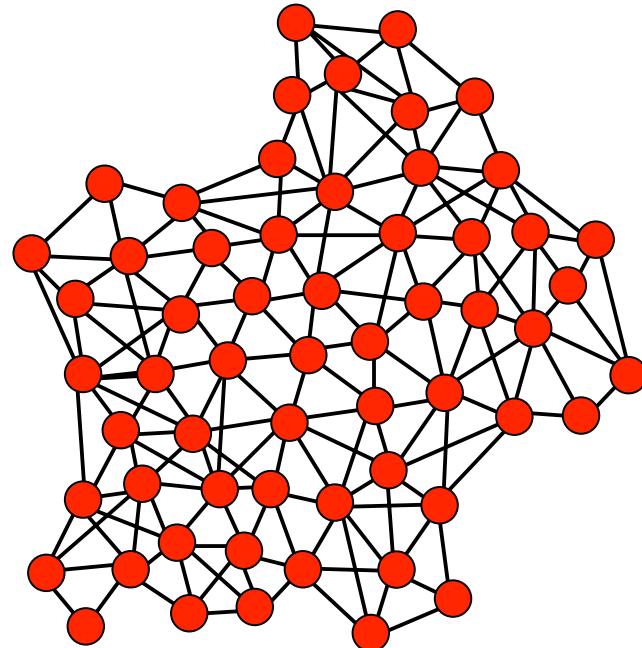
# Computing with fields



# Amorphous Medium



- Continuous space & time
- Infinite number of devices
- See neighbors' past state



- Approximate with:
- Discrete network of devices
- Signals transmit state

```
(def gradient (src) ...)
(def distance (src dst) ...)
(def dilate (src n)
  (<= (gradient src) n))
(def channel (src dst width)
  (let* ((d (distance src dst))
         (trail (<= (+ (gradient src)
                        (gradient dst))
                    d)))
    (dilate trail width)))
```

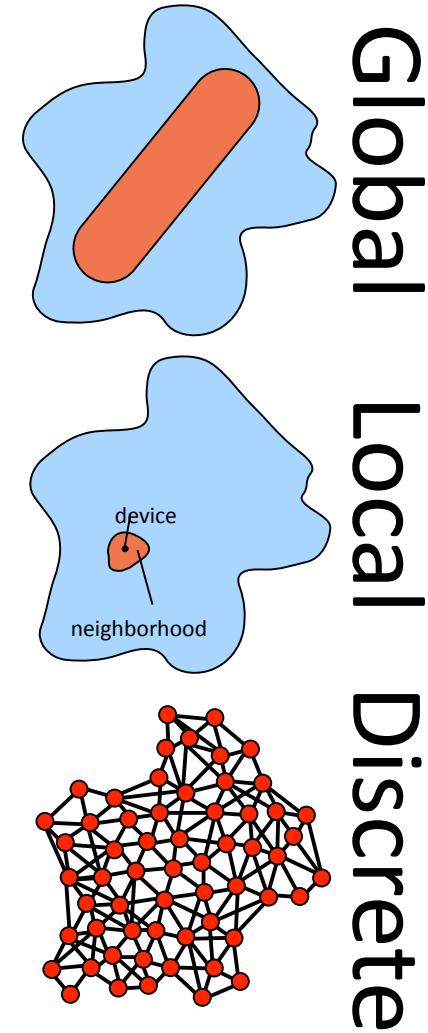
platform  
specificity &  
optimization

**evaluation**

global to local  
compilation

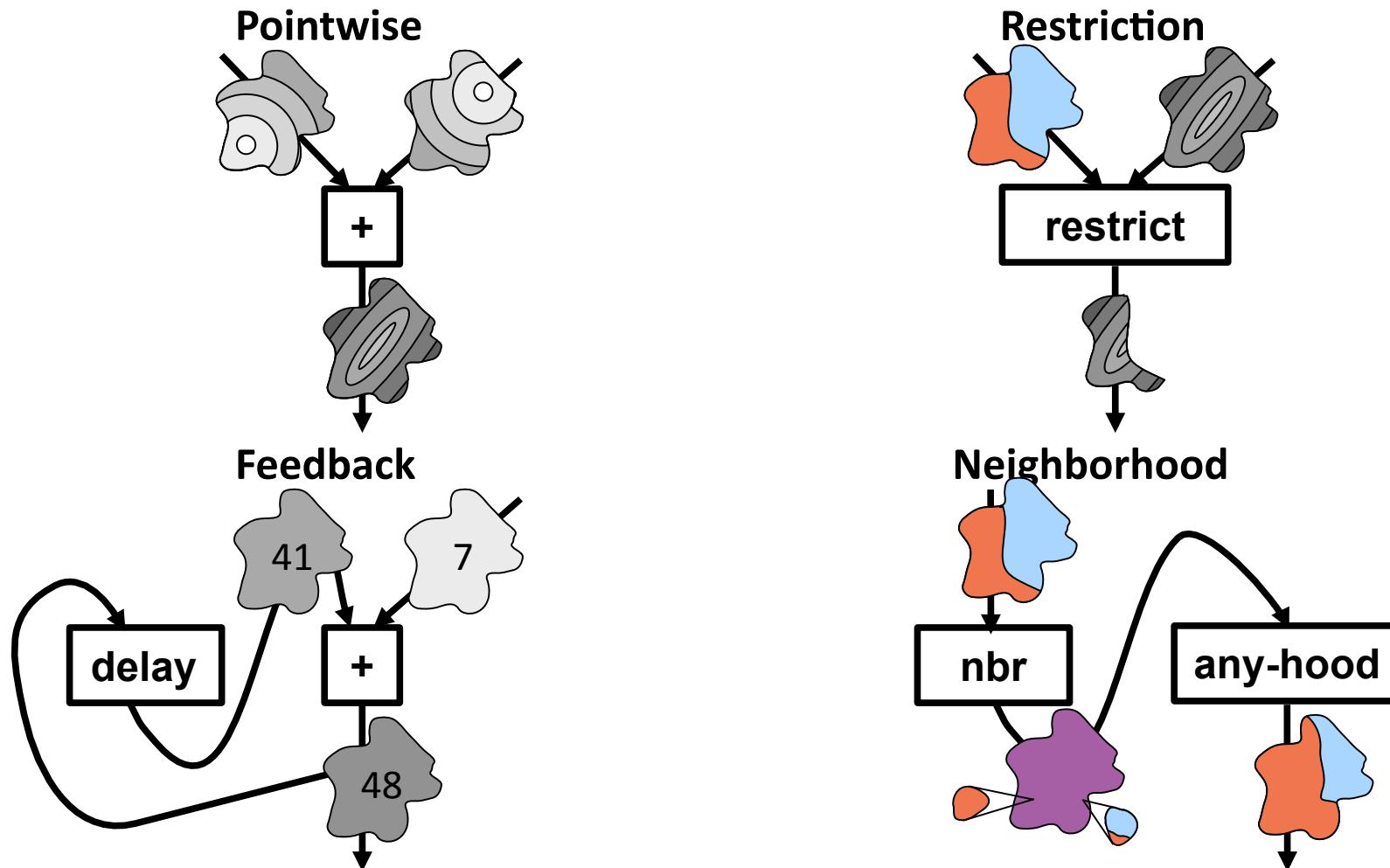
discrete  
approximation

Device  
Kernel

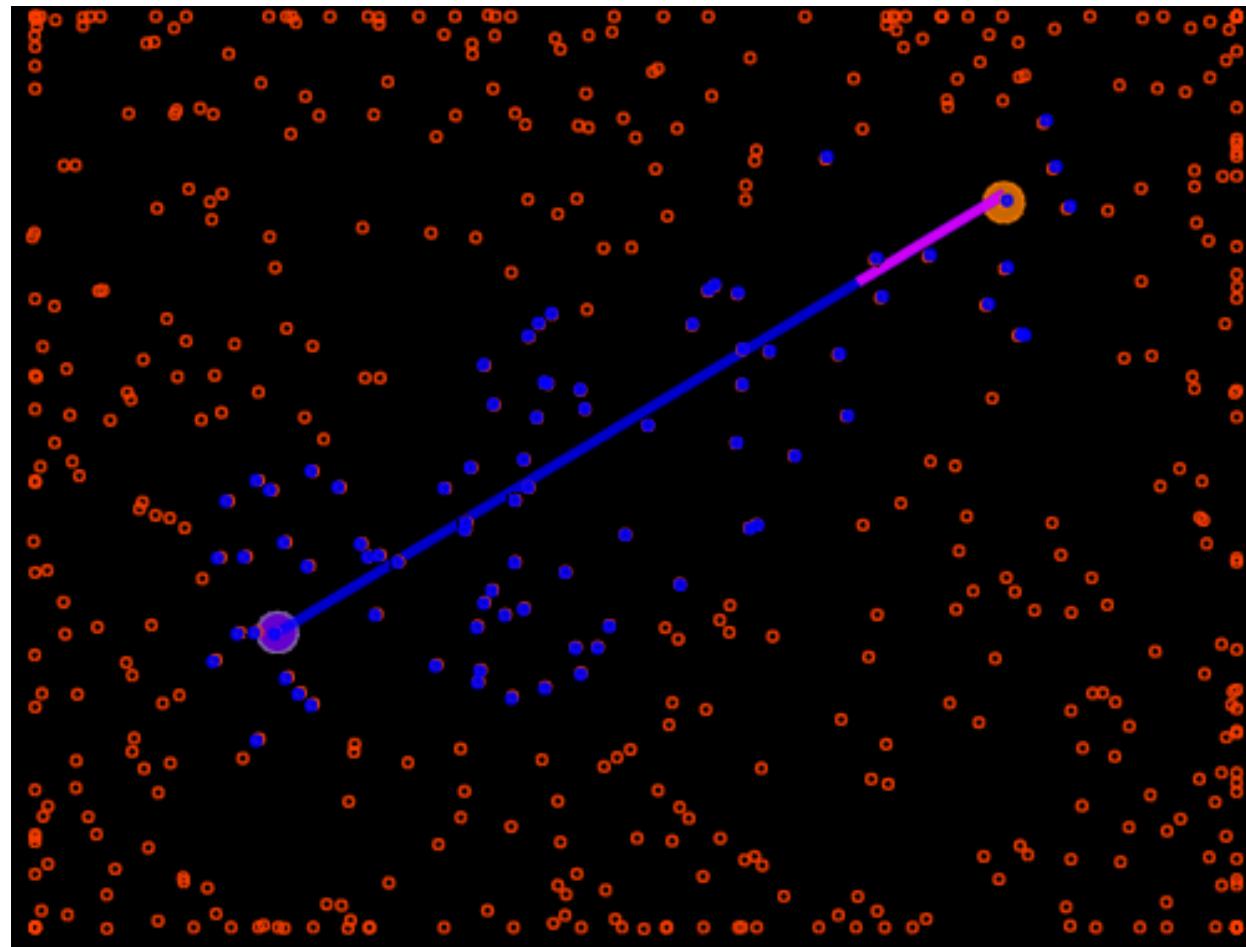


[Beal & Bachrach, '06]

# Proto's Families of Primitives



In simulation...



# Weaknesses

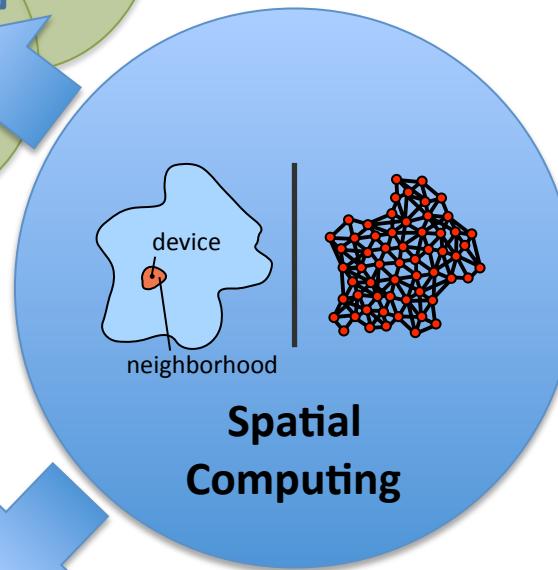
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- Programmers can break the abstraction
  - Functional programming scares people
  - No dynamic allocation of processes
  - No formal proofs available for quality of approximation in a composed program
- 
- The diagram consists of four vertical brackets on the right side of the slide. From top to bottom:
  - A green bracket groups the first two items: "Programmers can break the abstraction" and "Functional programming scares people".
  - A blue bracket groups the next two items: "No dynamic allocation of processes" and "No formal proofs available for quality of approximation in a composed program".
  - A red bracket groups the last two items: "By design Upgrades Coming Soon!" and "Active research area".

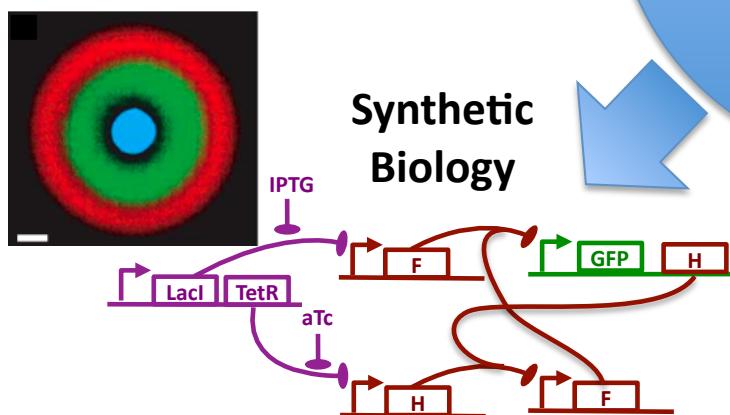
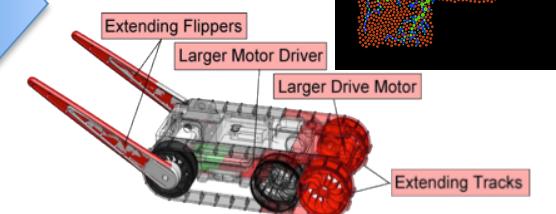


### Distributed Power Demand Response

*How can millions of appliances coordinate to change how we use energy?*



### Morphogenetic Engineering

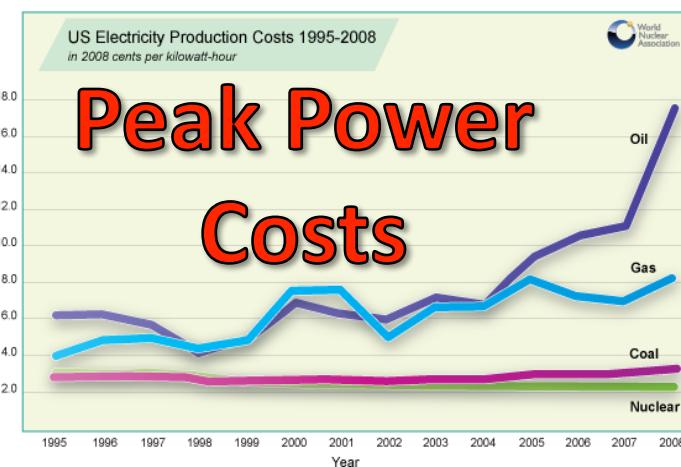


### Synthetic Biology

# Distributed Power Demand Response



Why is DR important?



# Inefficiency of Demand vs. Intention

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- Demand/supply mismatch is extremely costly
  - \$ billions to utilities, local governments
- Consumers dramatically reduce demand when:
  - ... aware of actual appliance energy use
  - ... informed about neighbors' energy use
  - ... aware of stress on power grid

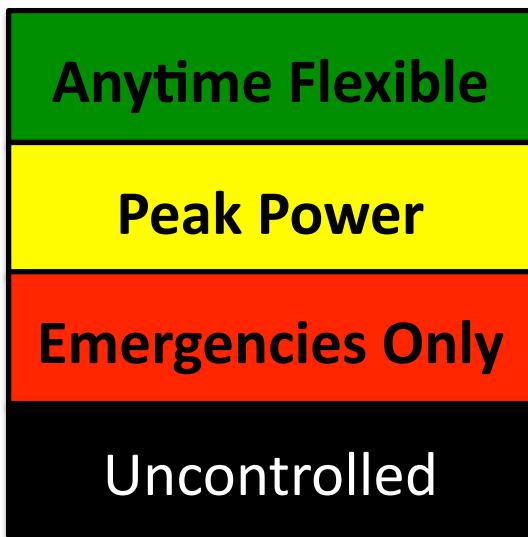
*Coordination opportunity: peak-shaving & demand management by **automating volunteerism***

# Key Challenges

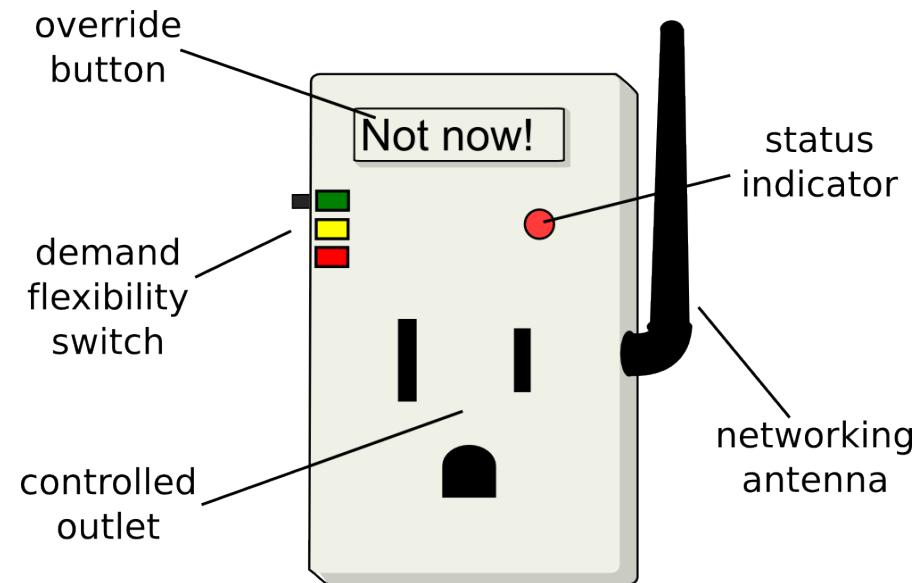
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- Scalability:
  - Safe, reliable coordinated response from millions of devices in <5 minutes
- Consumer interface:
  - High benefit, low “annoyance factor”
  - Eliciting useful information
  - Privacy concerns
- Deployability:
  - Technology alignment with market structure
  - Low cost devices
  - Market fragmentation across grid & in home

# Capturing User Requirements

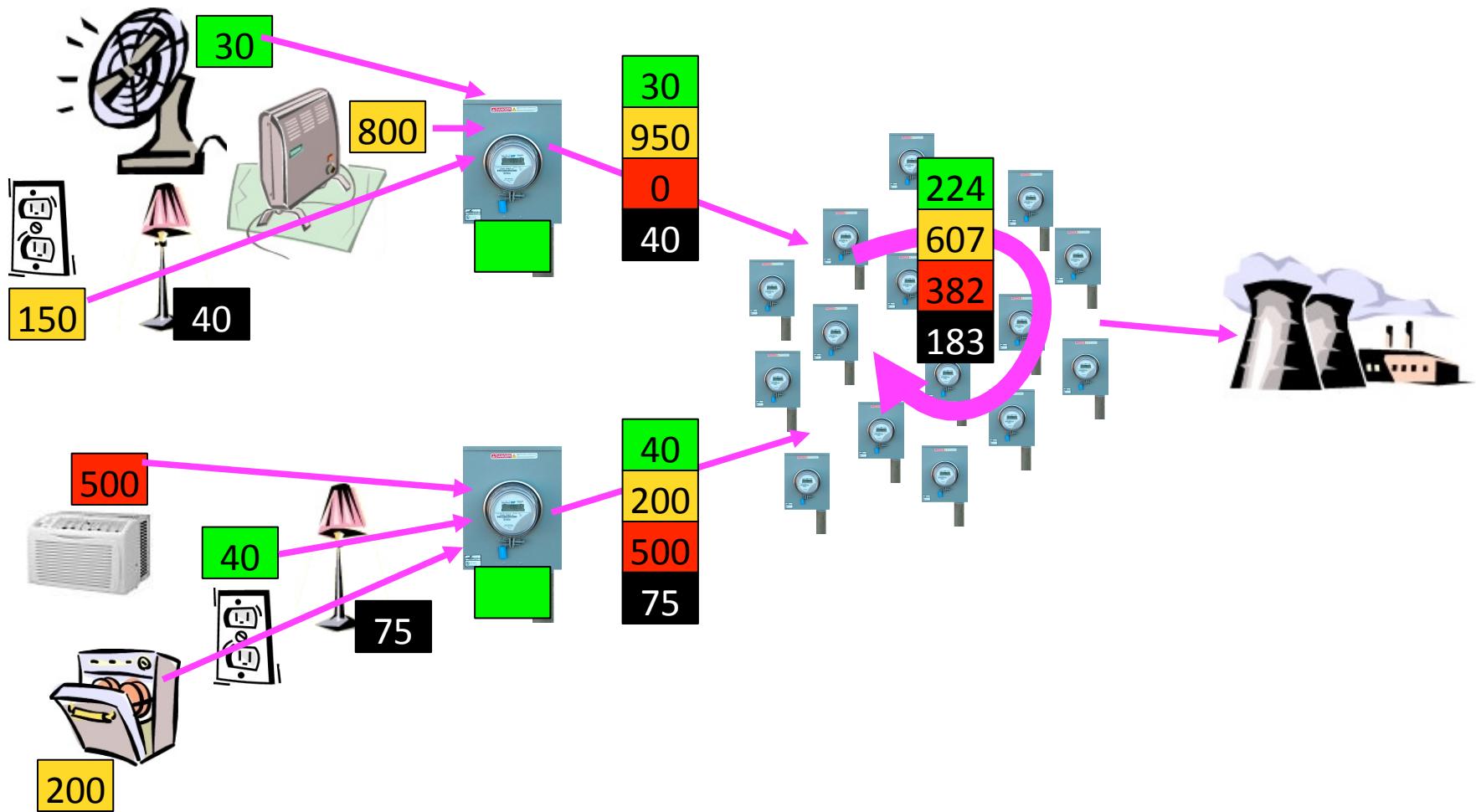


Qualitative  
Energy Flexibility

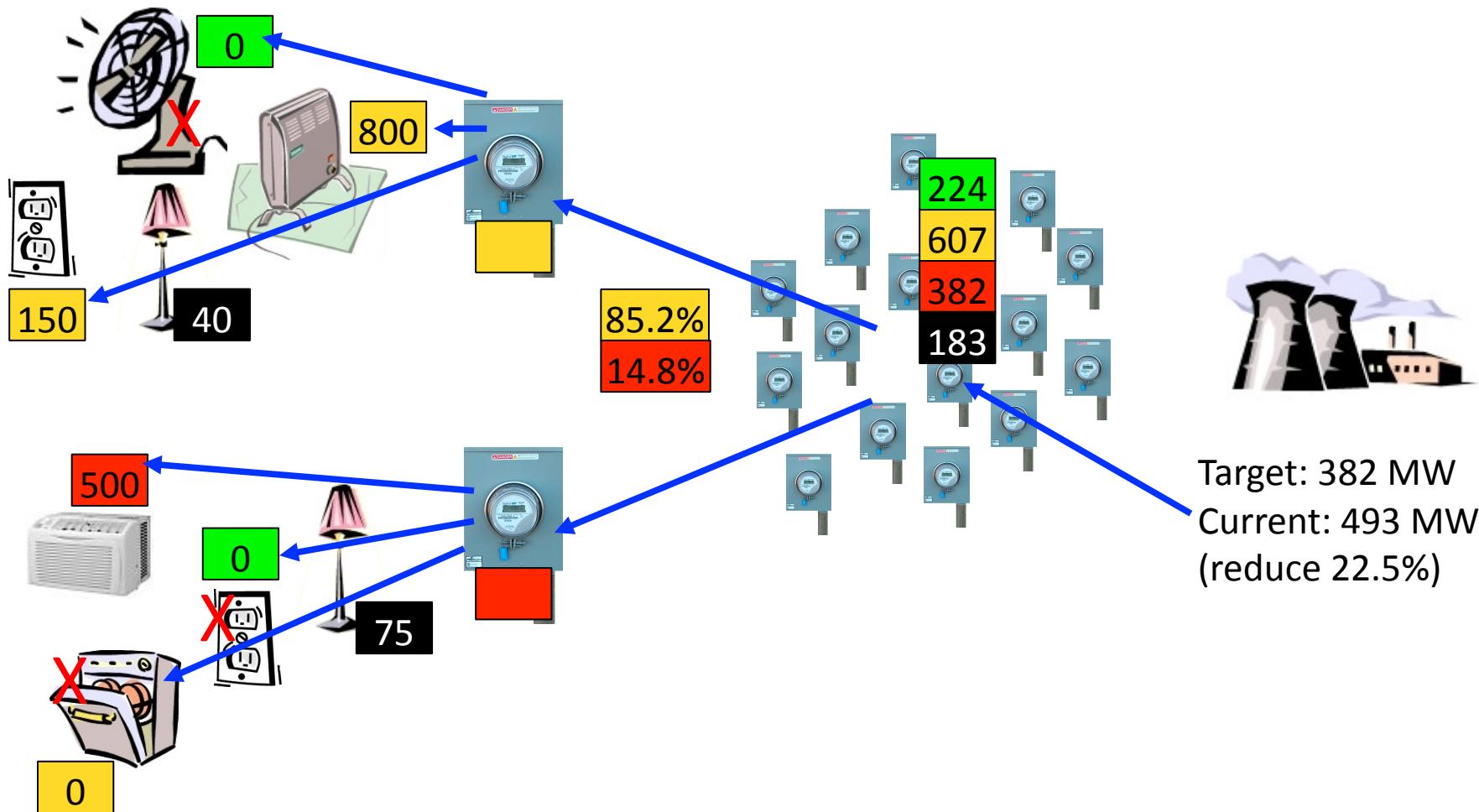


Smart plugs, new appliances,  
home automation, ...

# Distributed Creation of Aggregate Model



# Model Coordinates Local Control Actions



# ColorPower Algorithm

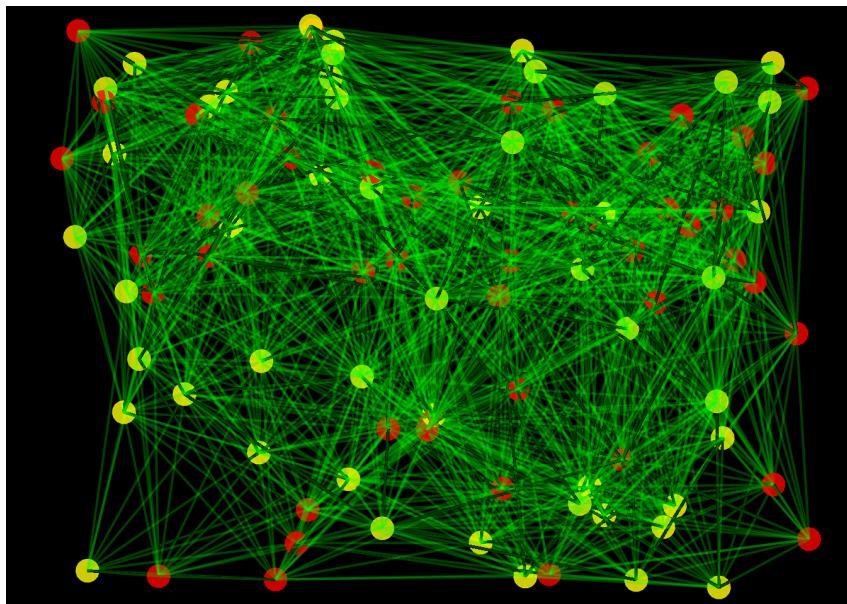
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- Challenge: fast, private, robust, non-intrusive
- Approach: randomized distributed control
  - Aggregate flexibility information to shared model
  - Disseminate control signals via gossip
  - Local decision; coin-flip for fractional color
  - Weight for availability, overdamped control

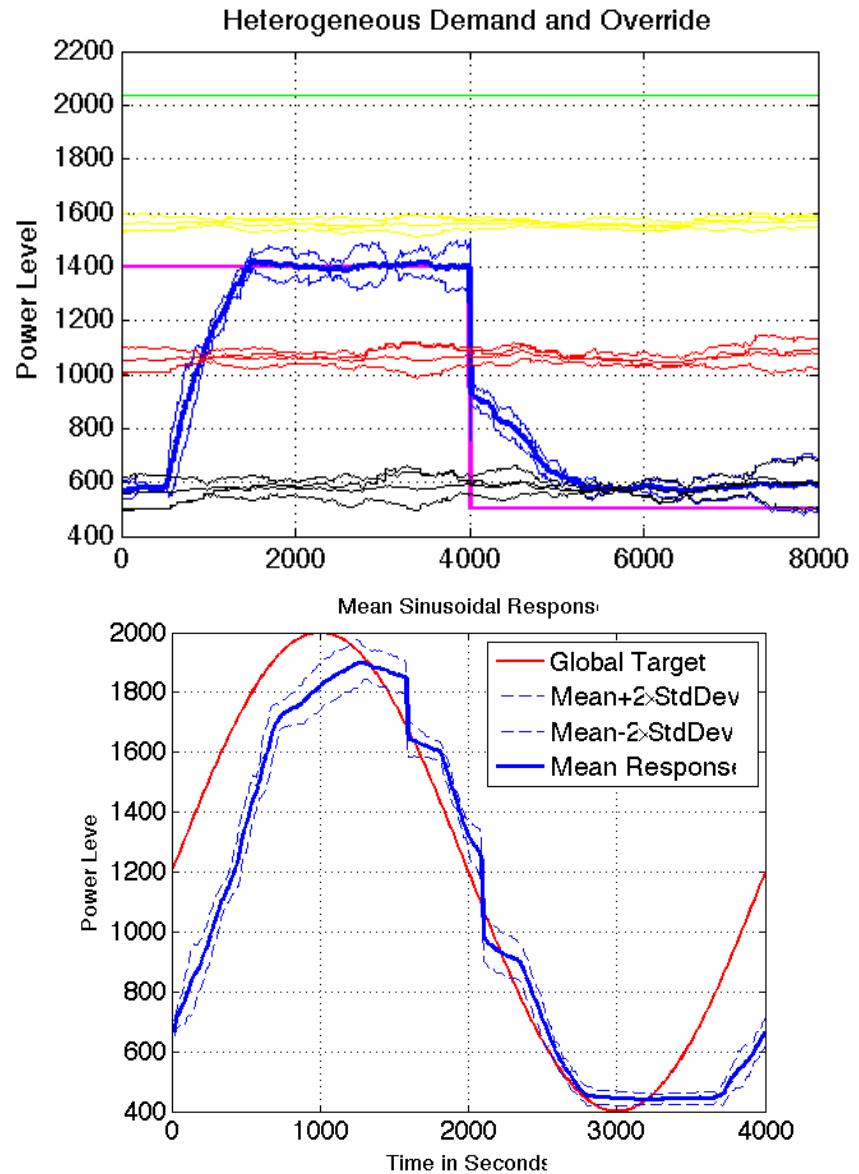
*Control problem: long timeouts on state changes*

# ColorPower Initial Algorithm

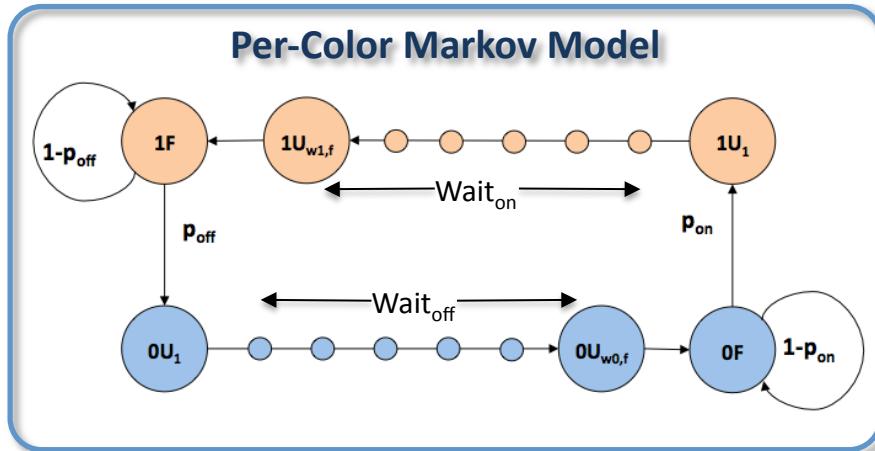
- Simulation on 100 device network using PID local controller



[Ranade & Beal, IEEE SASO 2010]



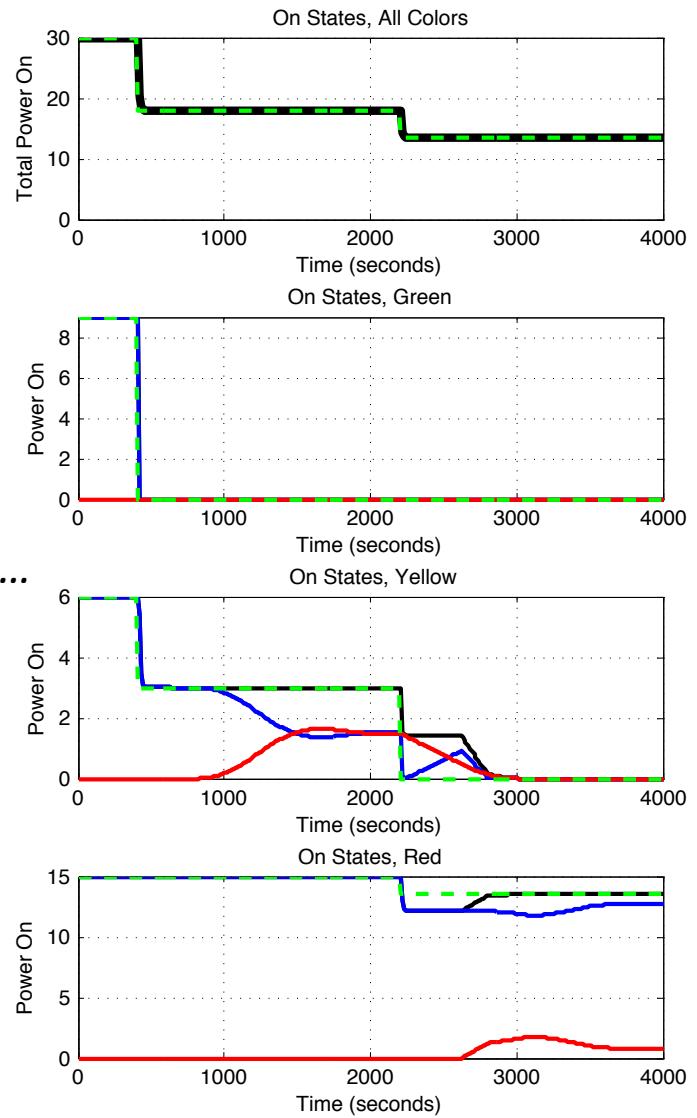
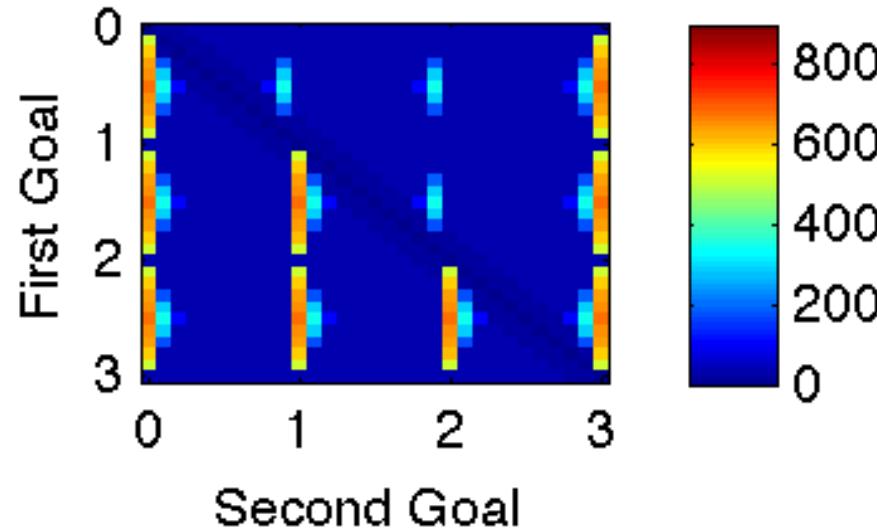
# Improved constraint-based controller



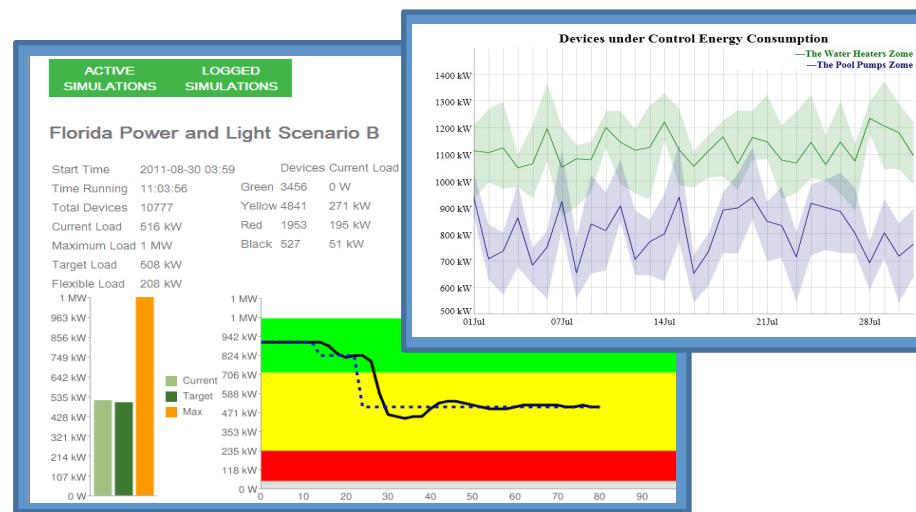
*Based on a Markov model of state flux...*

*... devices use constraint-based controls ...*

*... allowing <1 minute aggregate convergence time.*



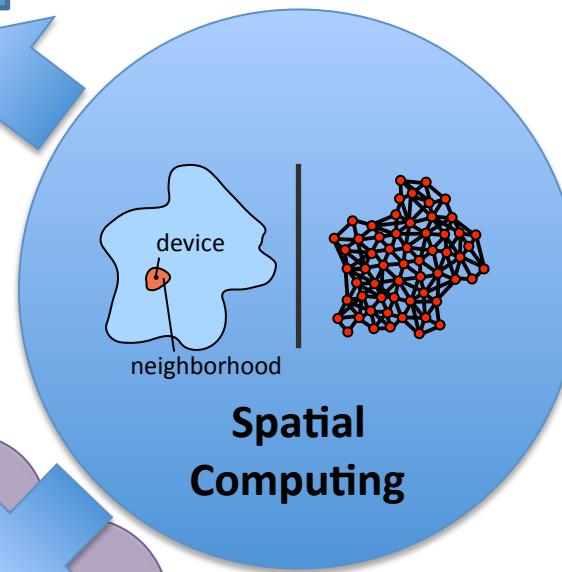
# Bringing it to the real world...



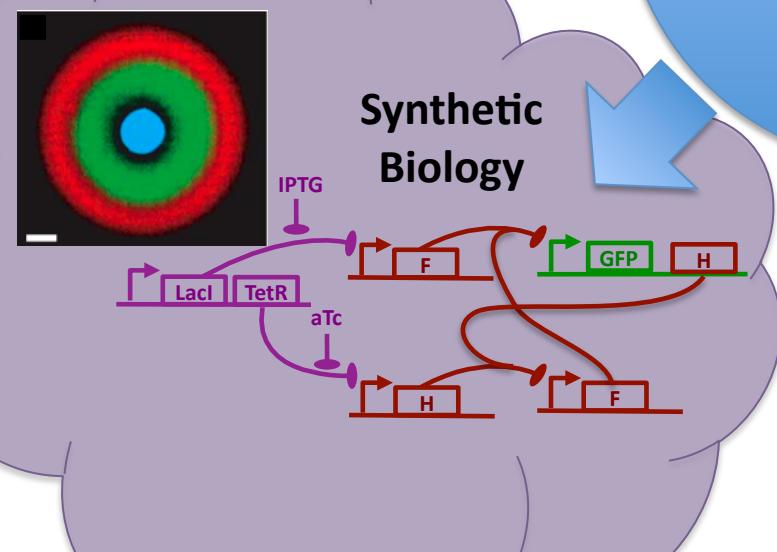
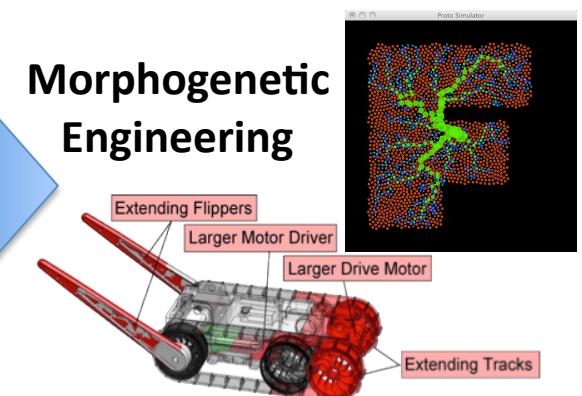
*Founded 2010 with team of serial entrepreneurs,  
well-funded, offices in San Francisco and  
Cambridge, first products in launch process...*



## Distributed Power Demand Response



## Morphogenetic Engineering

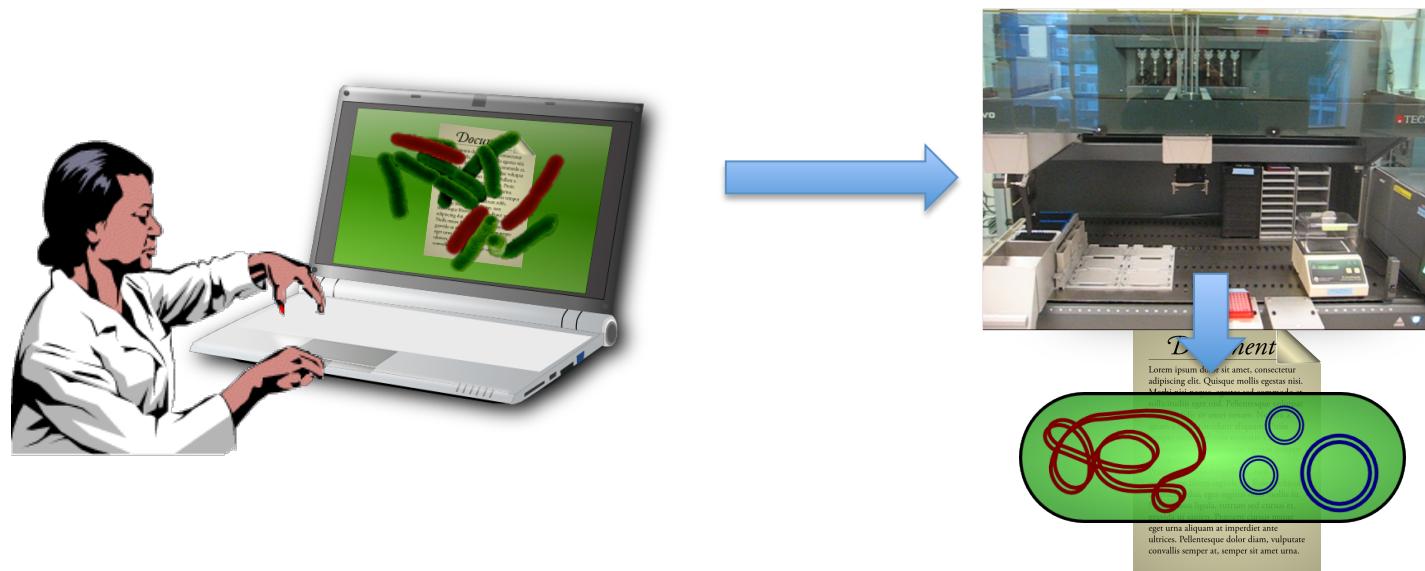


## Synthetic Biology

*How do you program the behavior of  $10^{12}$  cells?*

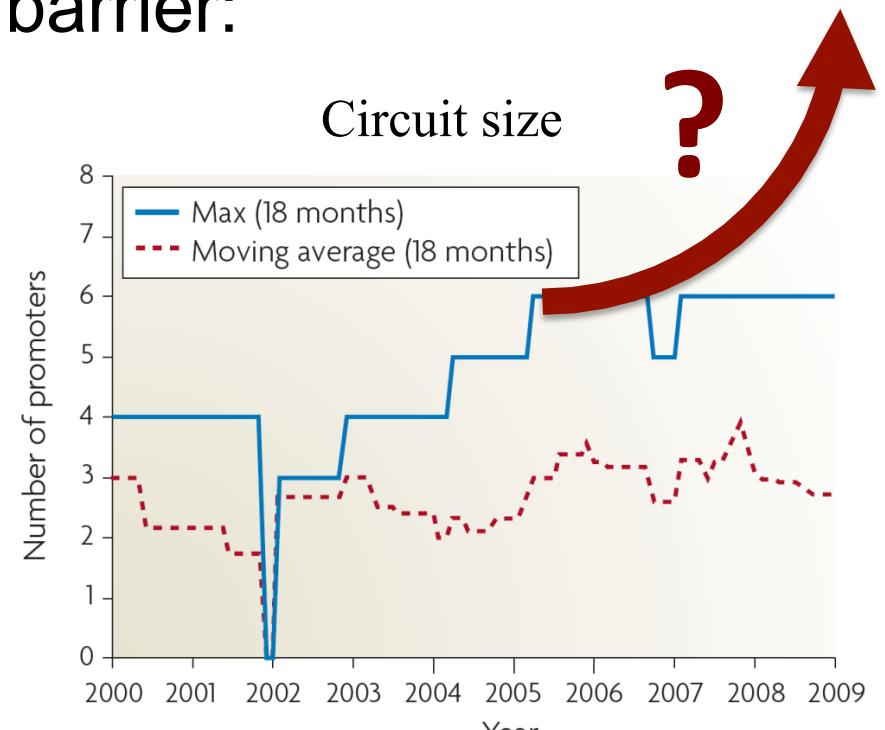
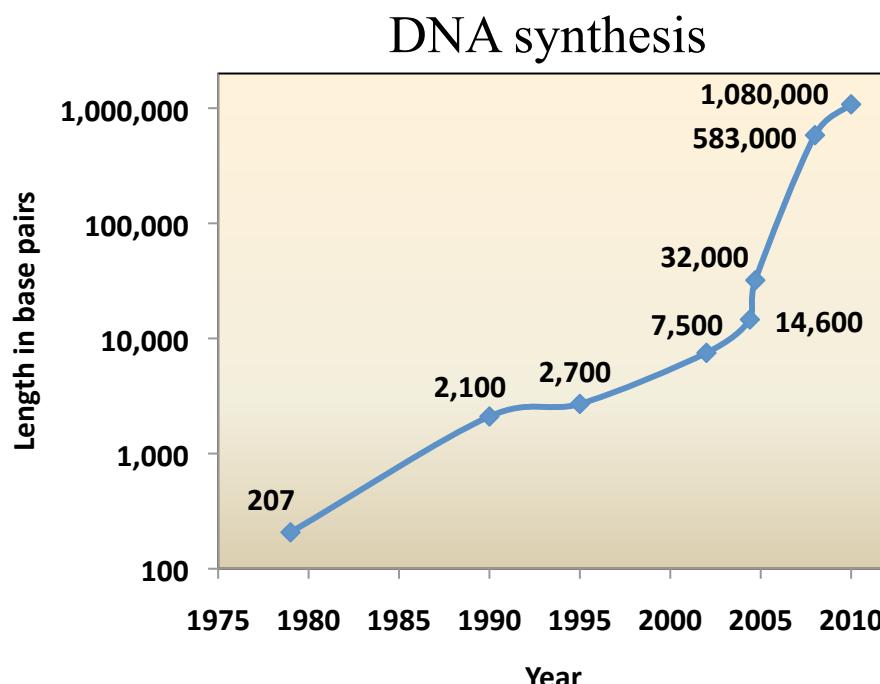
# Vision: WYSIWYG Synthetic Biology

Bioengineering should be like document preparation:



# Why is this important?

- Breaking the complexity barrier:



[Purnick & Weiss, '09]

- Multiplication of research impact
- Reduction of barriers to entry

\*Sampling of systems in publications with experimental circuits

# Why a tool-chain?

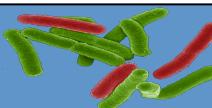
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Organism Level Description

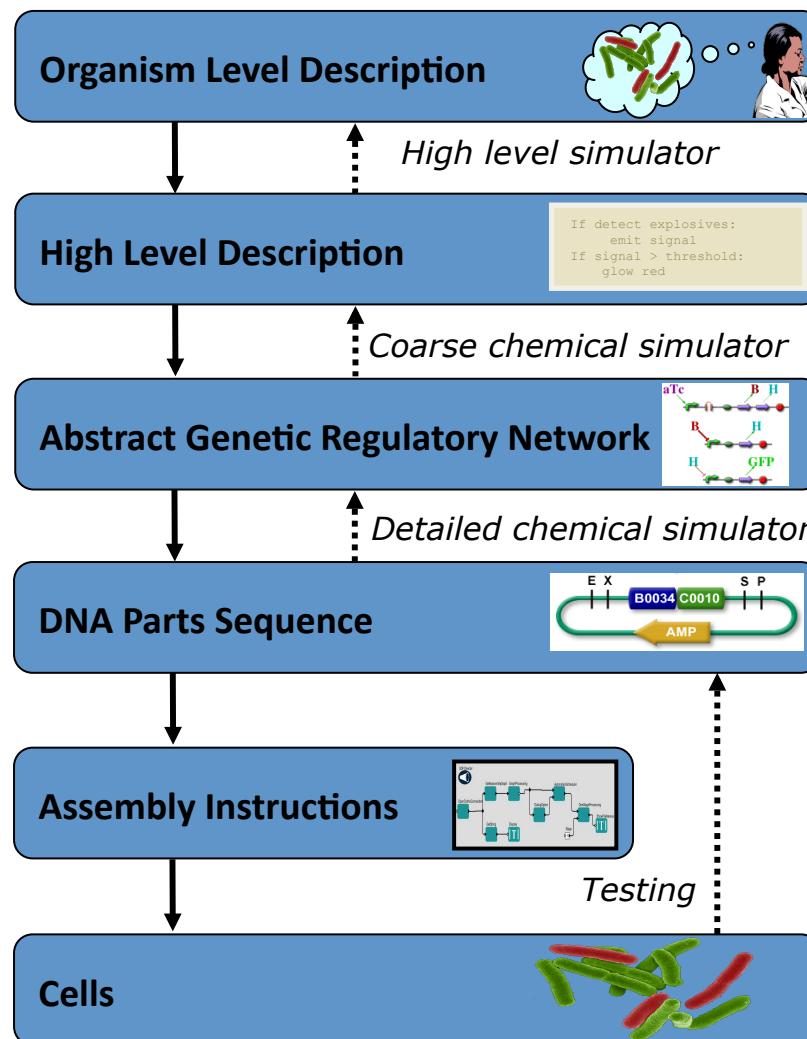


*This gap is too big  
to cross with a  
single method!*

Cells



# The TASBE architecture:



Collaborators:



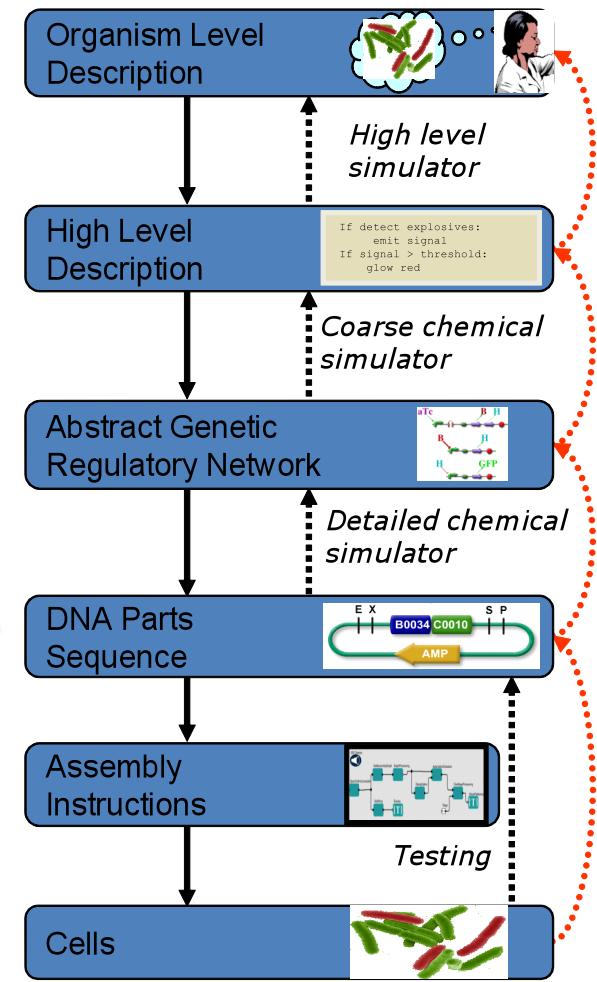
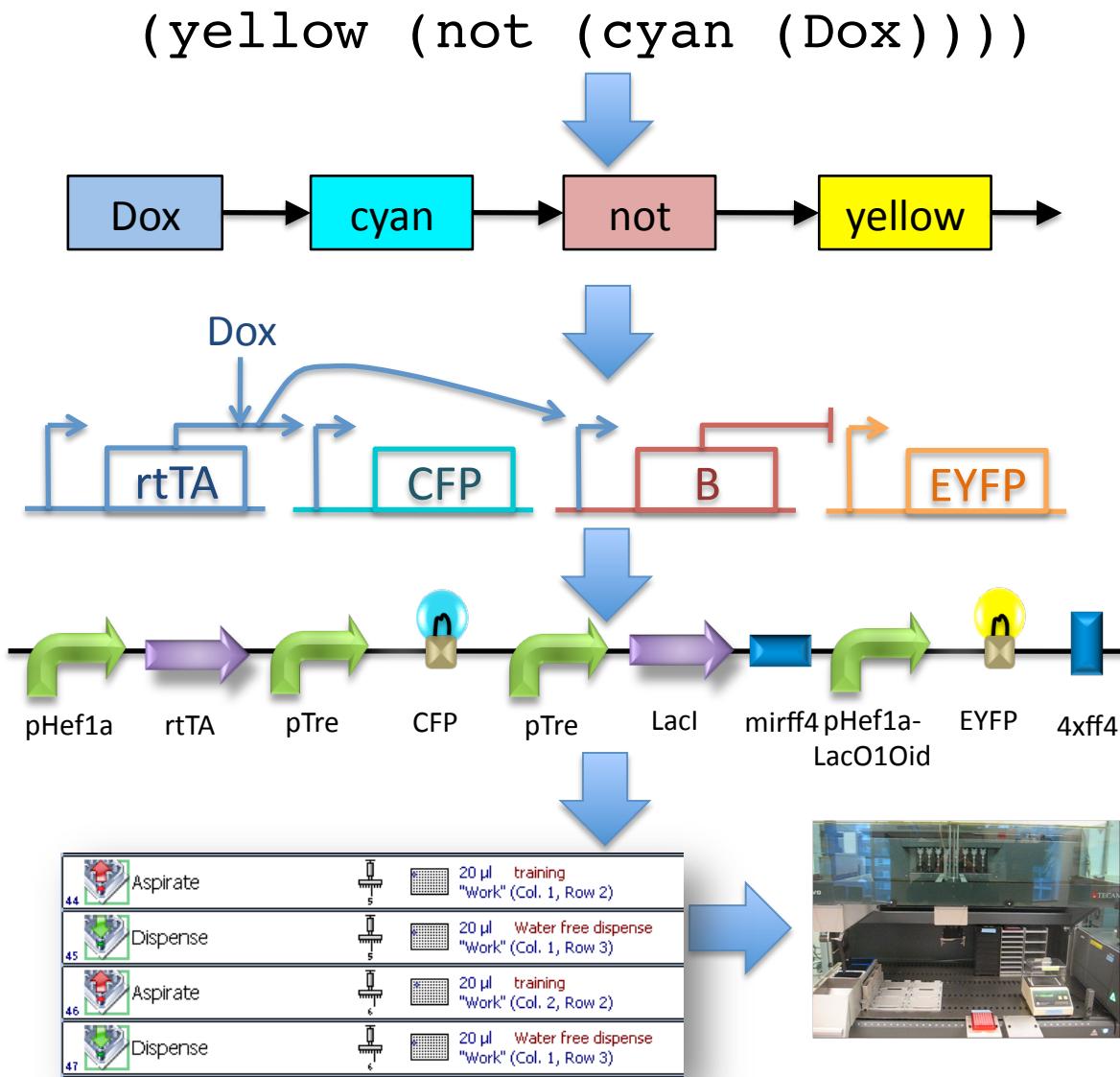
Ron  
Weiss



Douglas  
Densmore

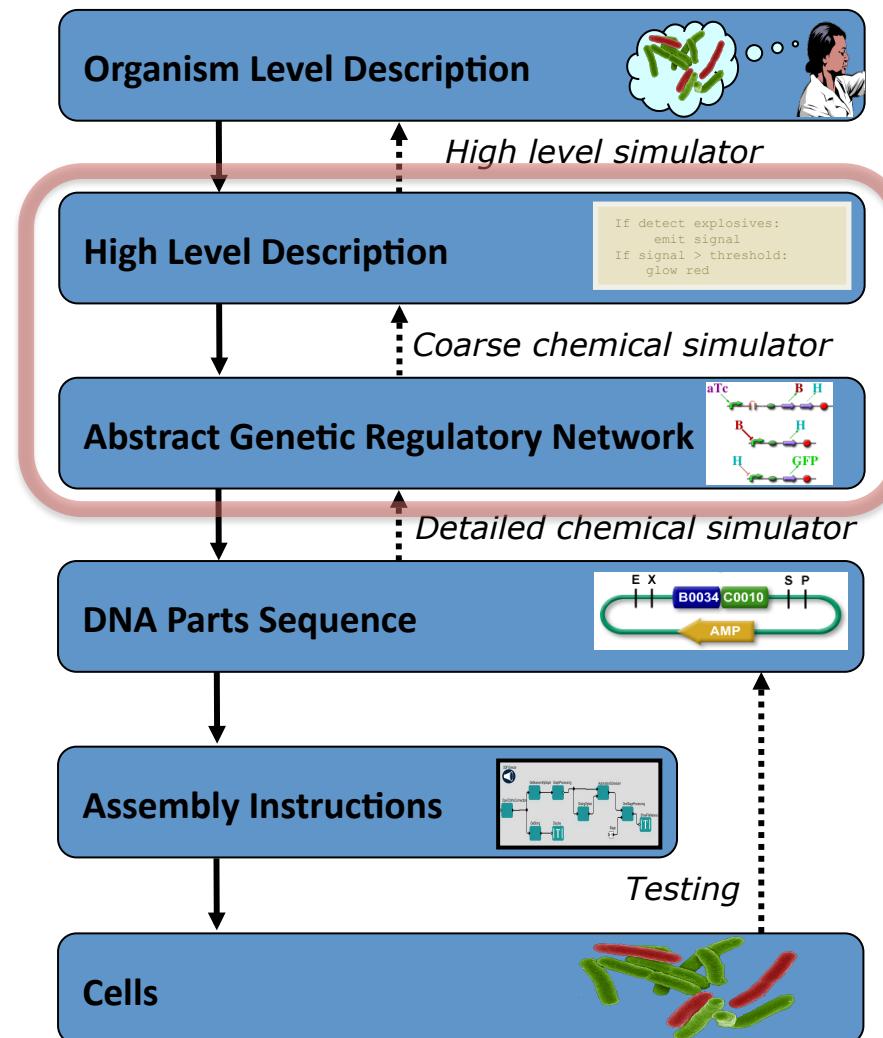
*Modular architecture  
also open for flexible  
choice of organisms,  
protocols, methods, ...*

# A Tool-Chain Example

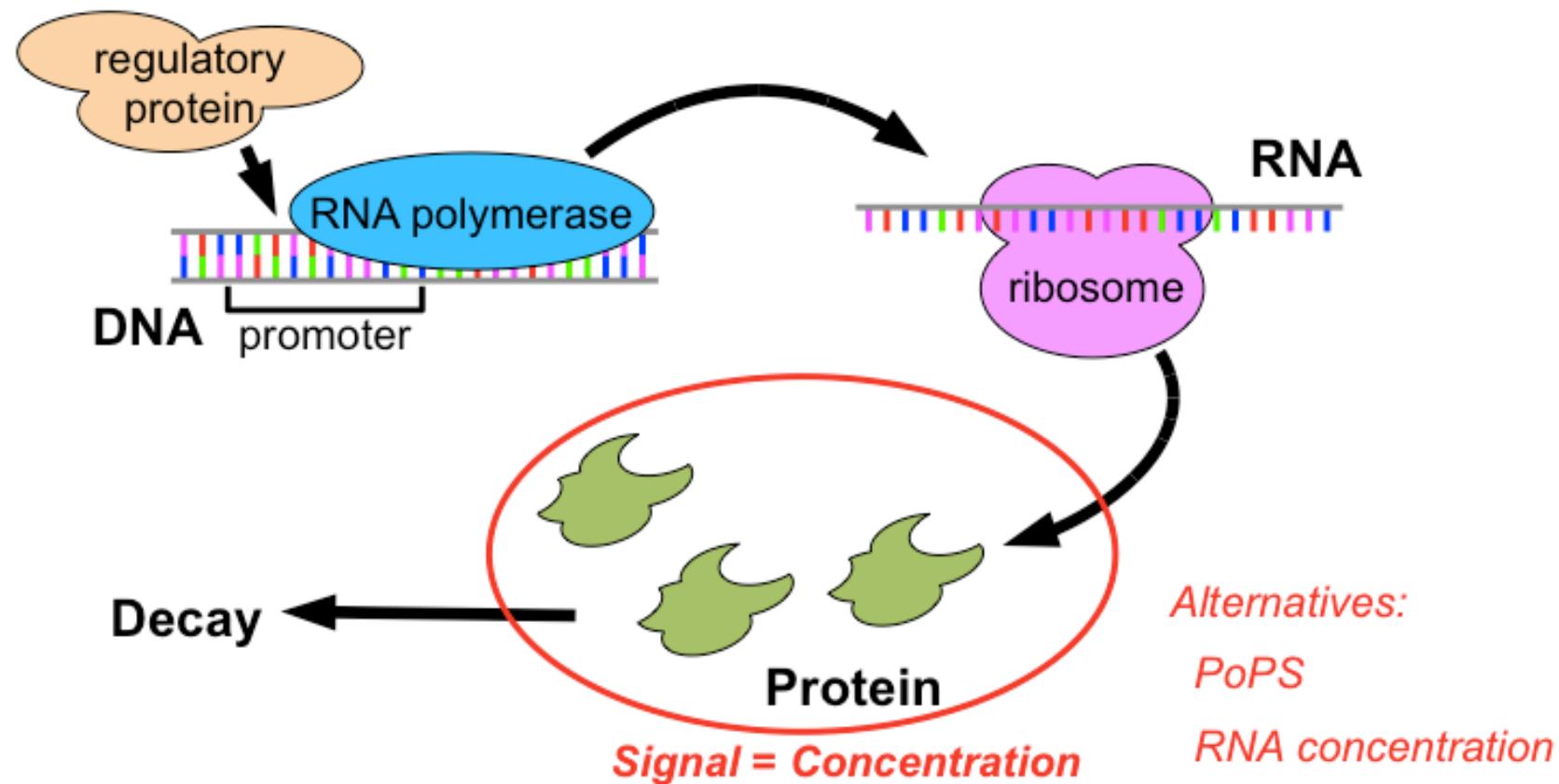


# Today's focus: BioCompiler

## Compilation & Optimization



# Transcriptional Logic

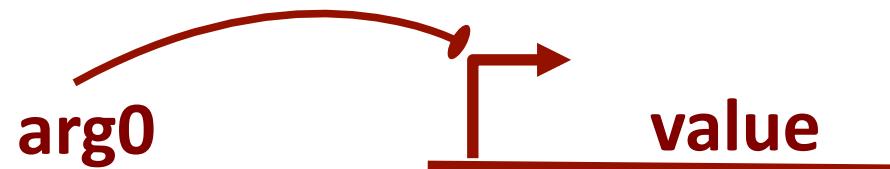


Stabilizes at  $\text{decay} = \text{production}$

# Motif-Based Compilation

- High-level primitives map to GRN design motifs
  - e.g. logical operators:

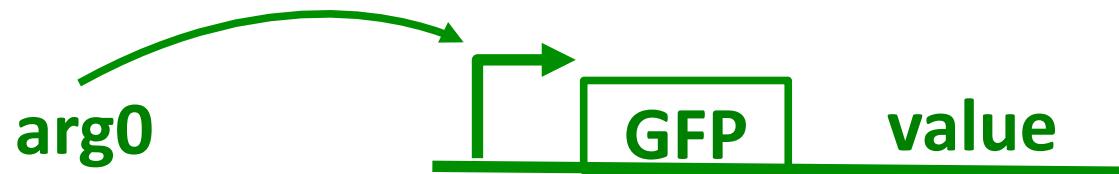
```
(primitive not (boolean) boolean  
:grn-motif ((P high R- arg0 value T)))
```



# Motif-Based Compilation

- High-level primitives map to GRN design motifs
  - e.g. logical operators, **actuators**:

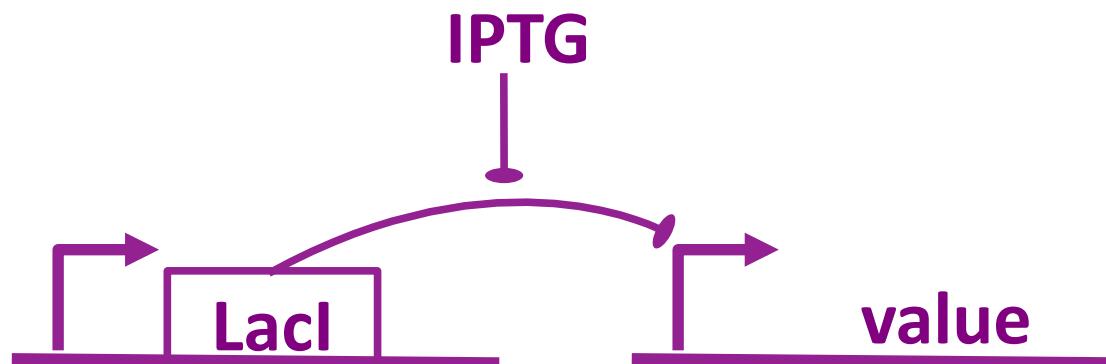
```
(primitive green (boolean) boolean :side-effect  
:type-constraints ((= value arg0))  
:grn-motif ((P R+ arg0 GFP|arg0 value T)))
```



# Motif-Based Compilation

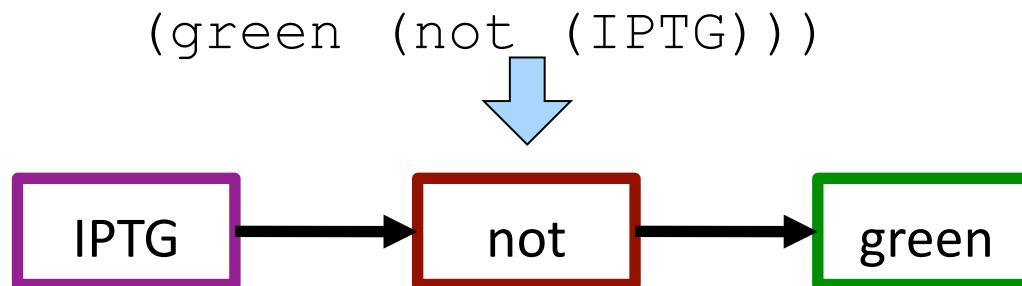
- High-level primitives map to GRN design motifs
  - e.g. logical operators, actuators, **sensors**:

```
(primitive IPTG () boolean  
  :grn-motif ((P high LacI|boolean T)  
    (RXN (IPTG|boolean) represses LacI)  
    (P high R- LacI value T)))
```



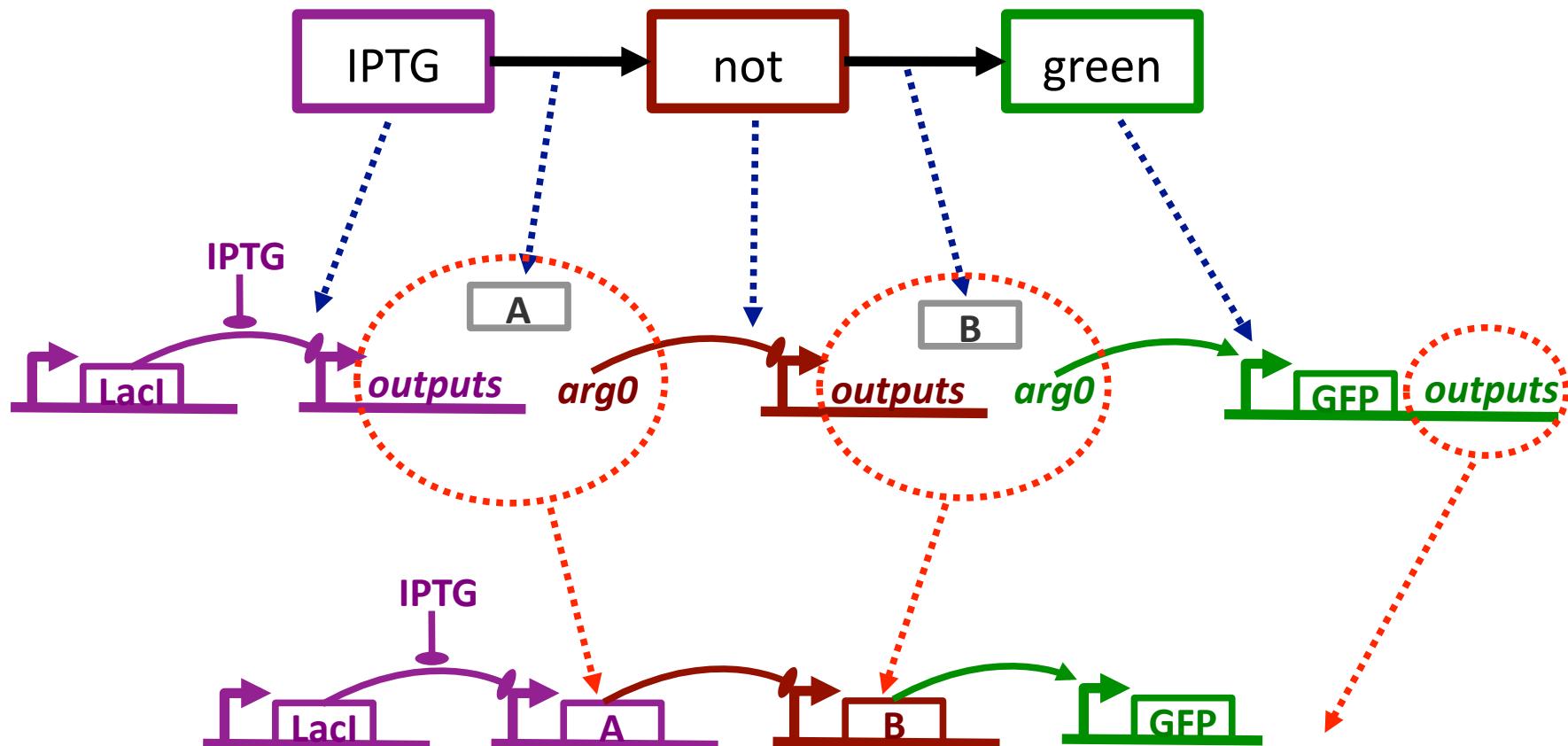
# Motif-Based Compilation

- Functional program gives dataflow computation:

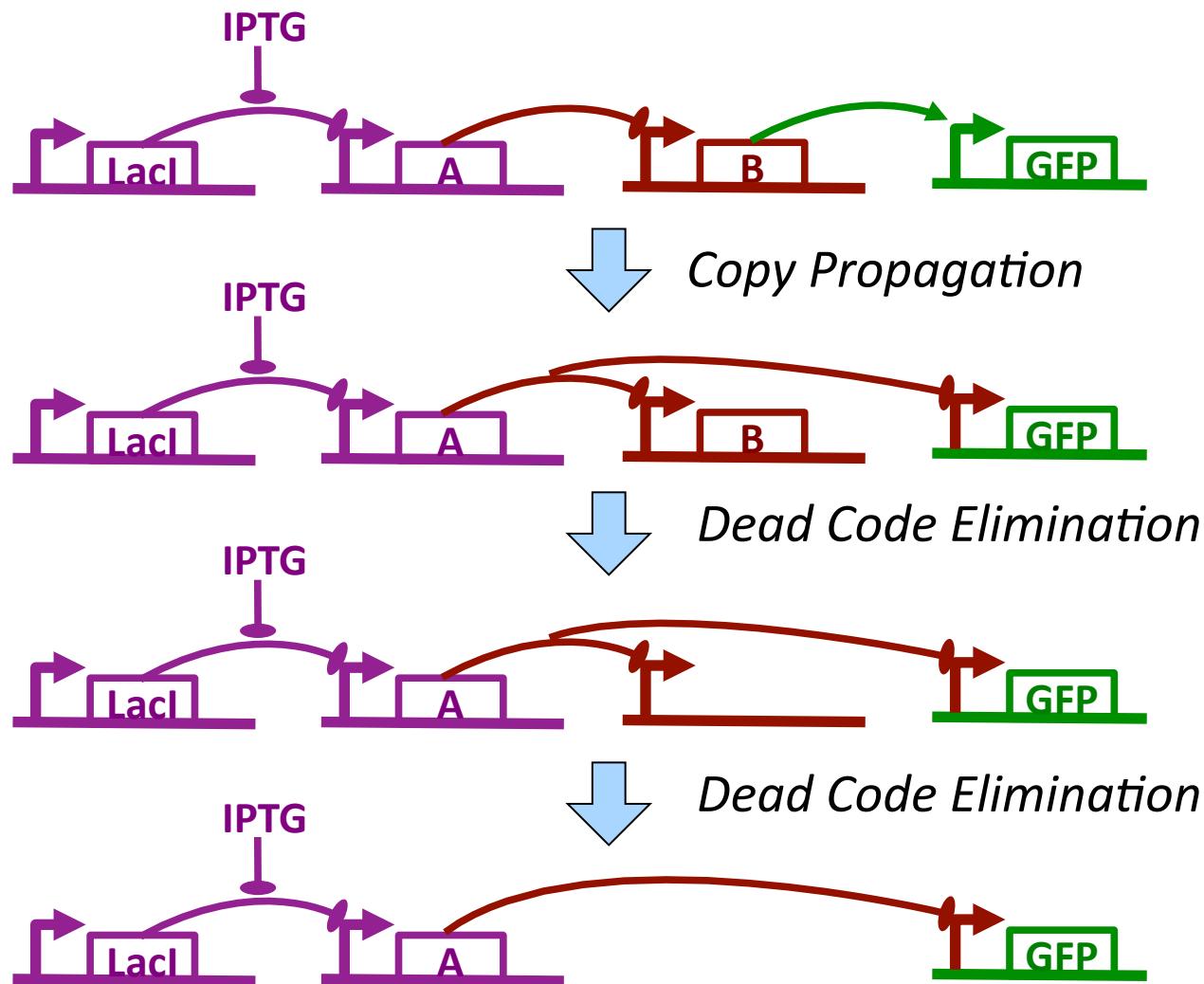


# Motif-Based Compilation

- Operators translated to motifs:



# Optimization



# Complex System: Feedback Latch

---

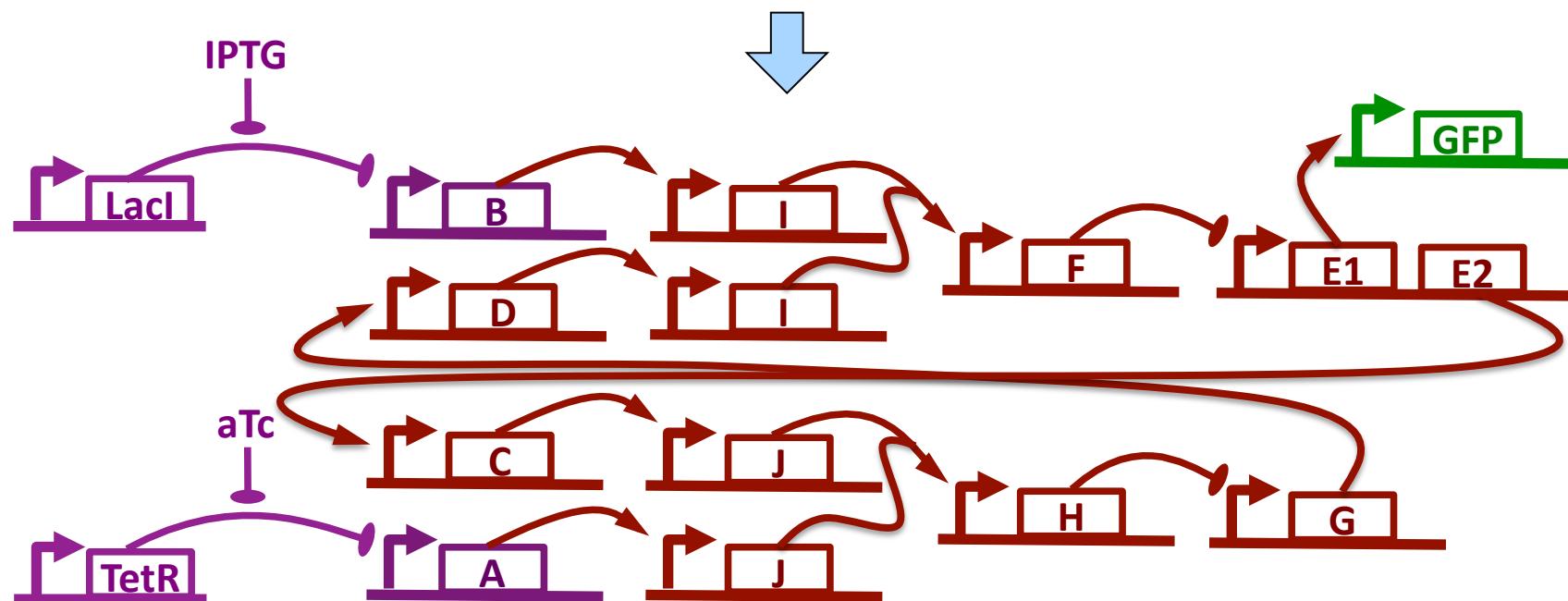
```
(def sr-latch (s r)
  (letfed+ ((o boolean (not (or r o-bar) ))
            (o-bar boolean (not (or s o) )) )
    o) )

(green (sr-latch (aTc) (IPTG)) ) )
```

# Complex System: Feedback Latch

```
(def sr-latch (s r)
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(green (sr-latch (aTc) (IPTG)))
```

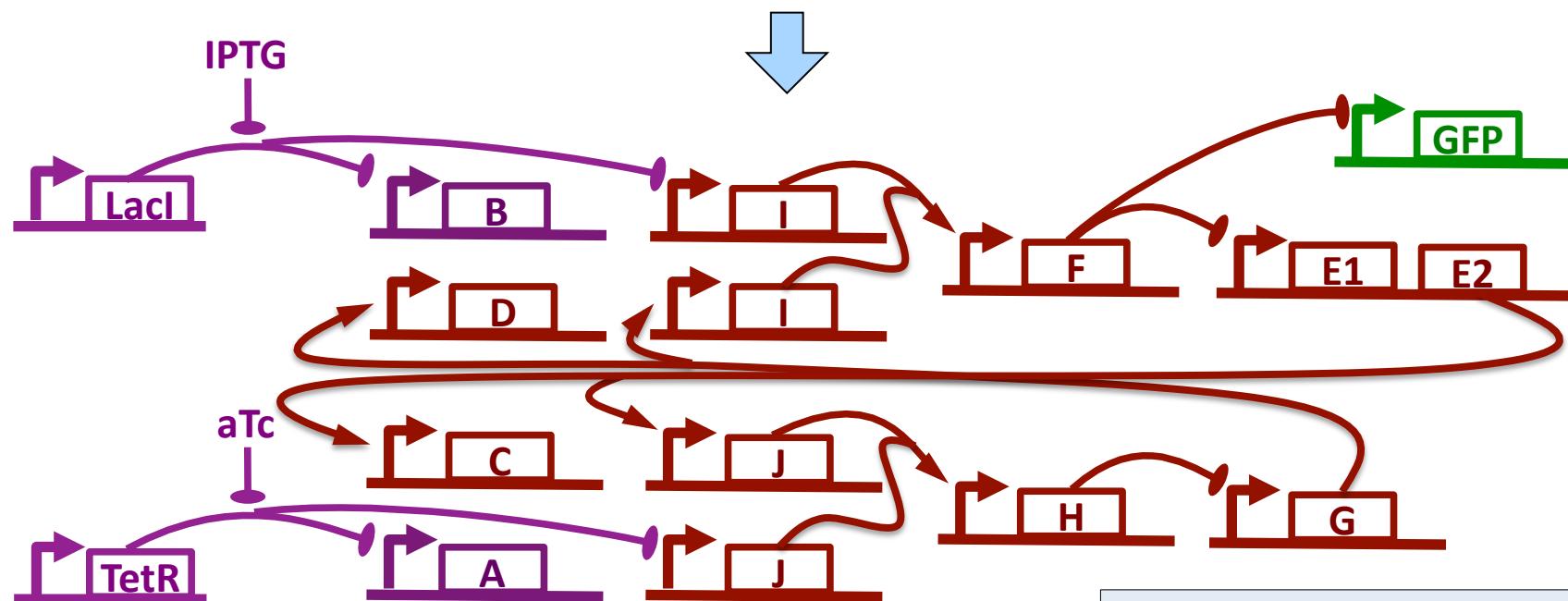


*Unoptimized: 15 functional units, 13 transcription factors*

# Optimization of Complex Designs

```
(def sr-latch (s r)
  (letfed+ ((o boolean (not (or r o-bar)))
            (o-bar boolean (not (or s o))))
    o))  

(green (sr-latch (aTc) (IPTG)))
```



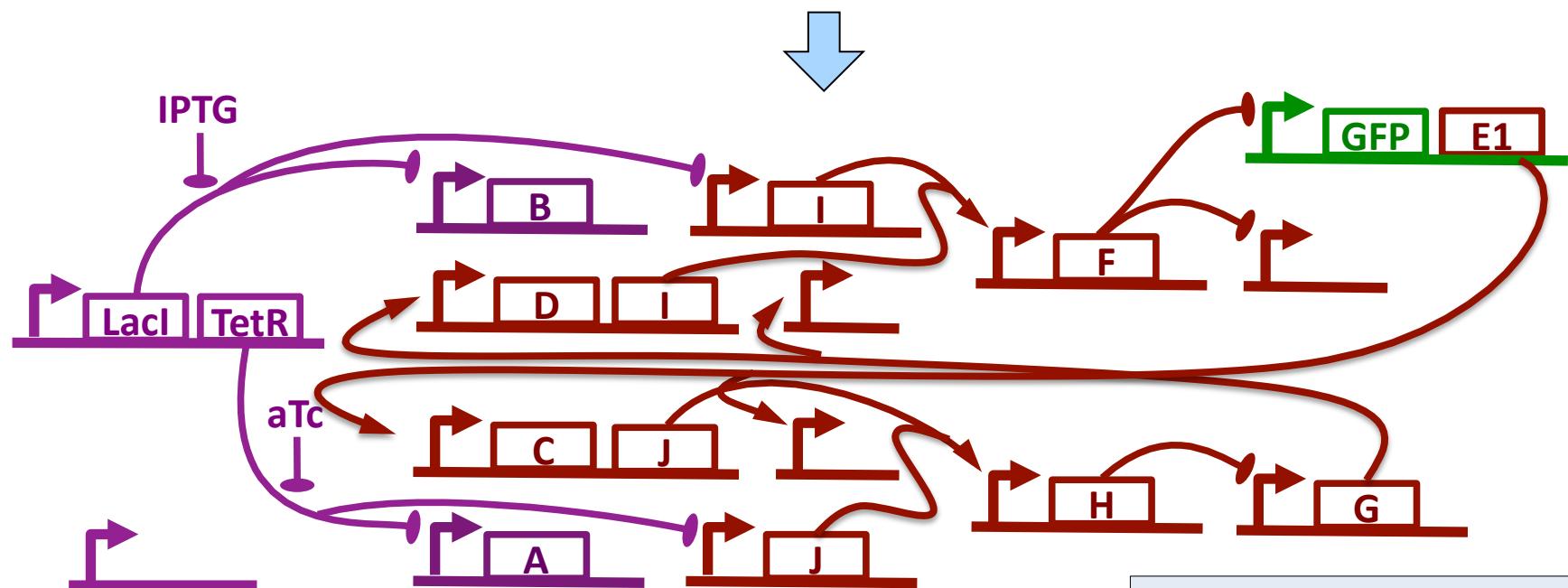
Unoptimized: 15 functional units, 13 transcription factors

*Copy Propagation*<sub>47</sub>

# Optimization of Complex Designs

```
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  (letfed+ ((o boolean (not (or r o-bar)))
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```



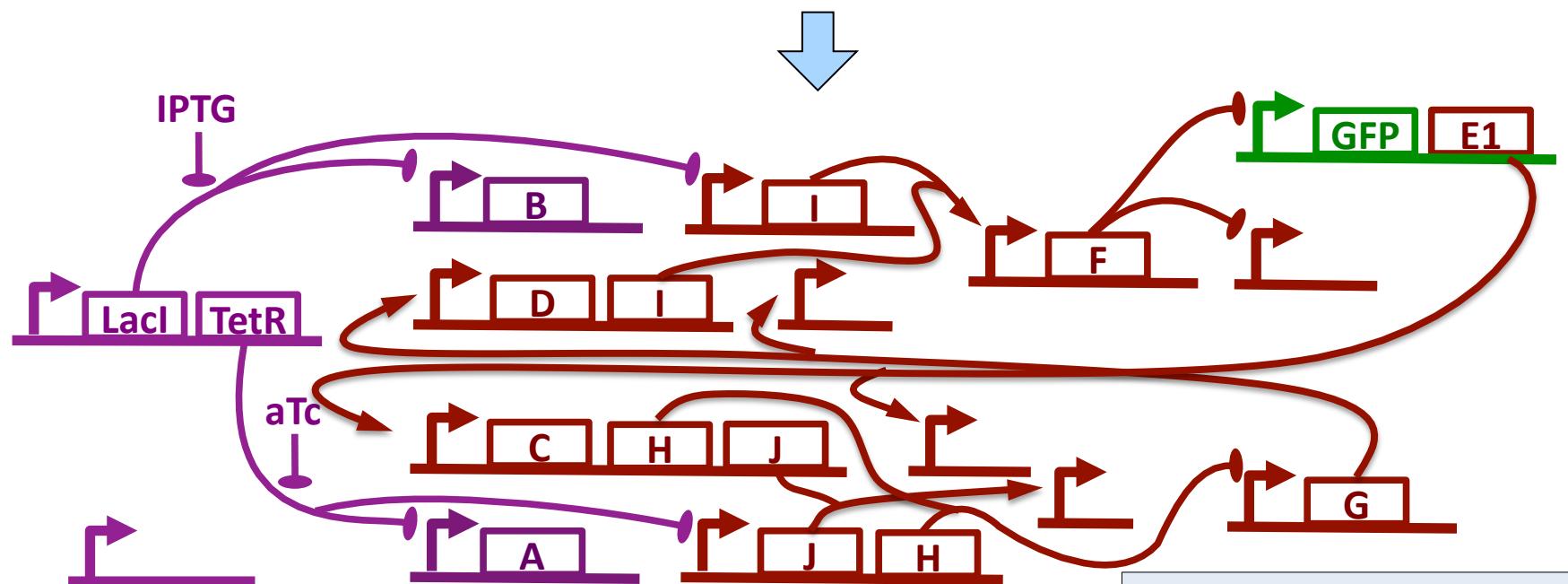
Unoptimized: 15 functional units, 13 transcription factors

**Common Subexp. Elim.**

# Optimization of Complex Designs

```
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            (o-bar boolean (not (or s o))))
    o))  

(green (sr-latch (aTc) (IPTG)))
```



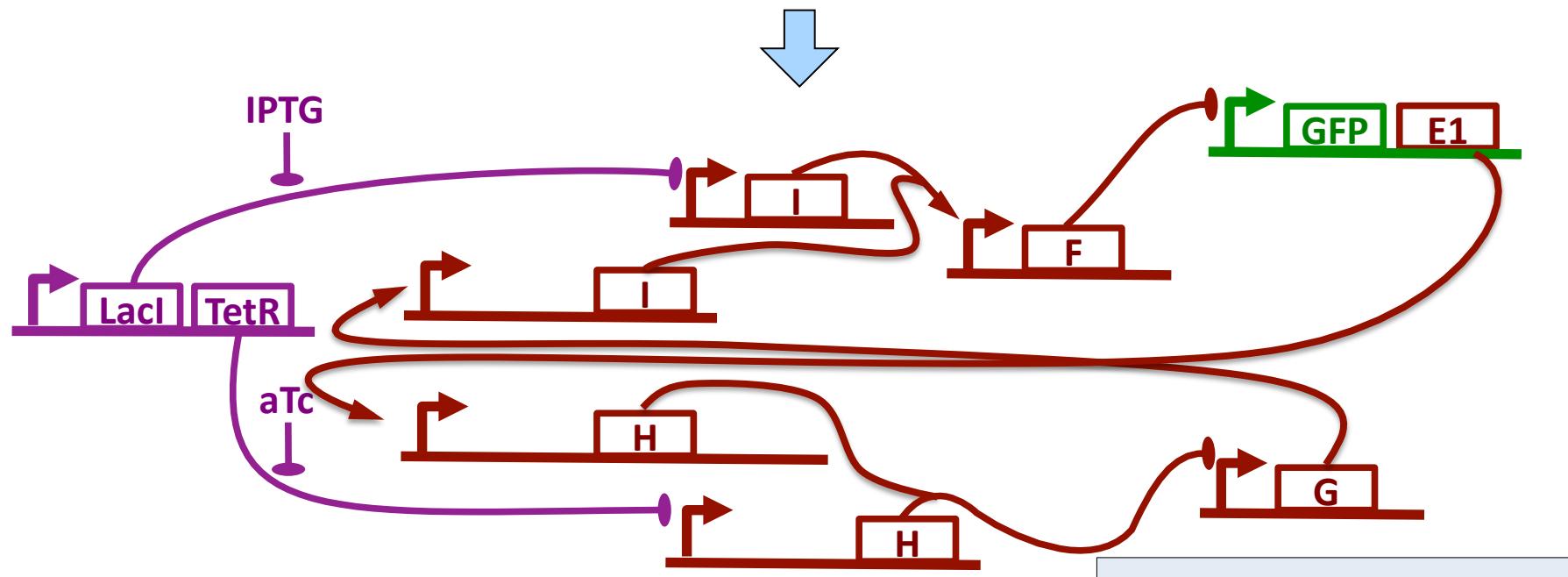
Unoptimized: 15 functional units, 13 transcription factors

**NOR Compression** 49

# Optimization of Complex Designs

```
(def sr-latch (s r)
  (letfed+ ((o boolean (not (or r o-bar)))
            (o-bar boolean (not (or s o))))
    o))  

(green (sr-latch (aTc) (IPTG)))
```



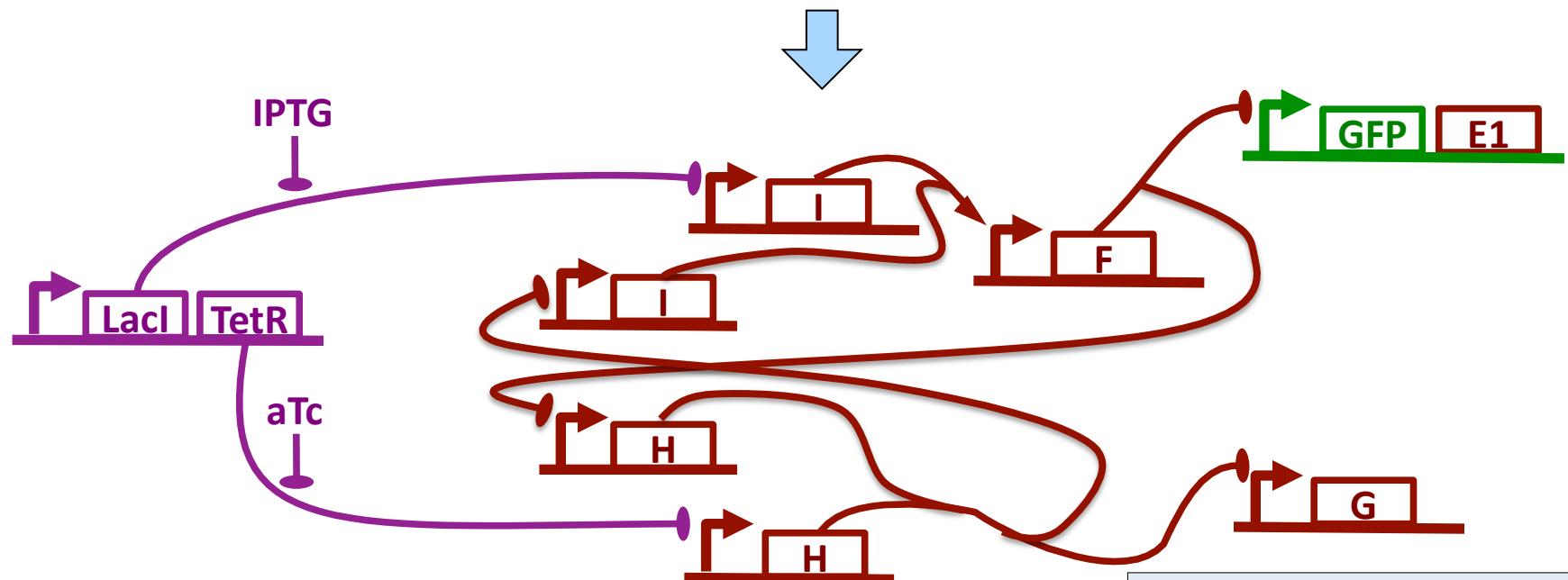
Unoptimized: 15 functional units, 13 transcription factors

**Dead Code Elimination**

# Optimization of Complex Designs

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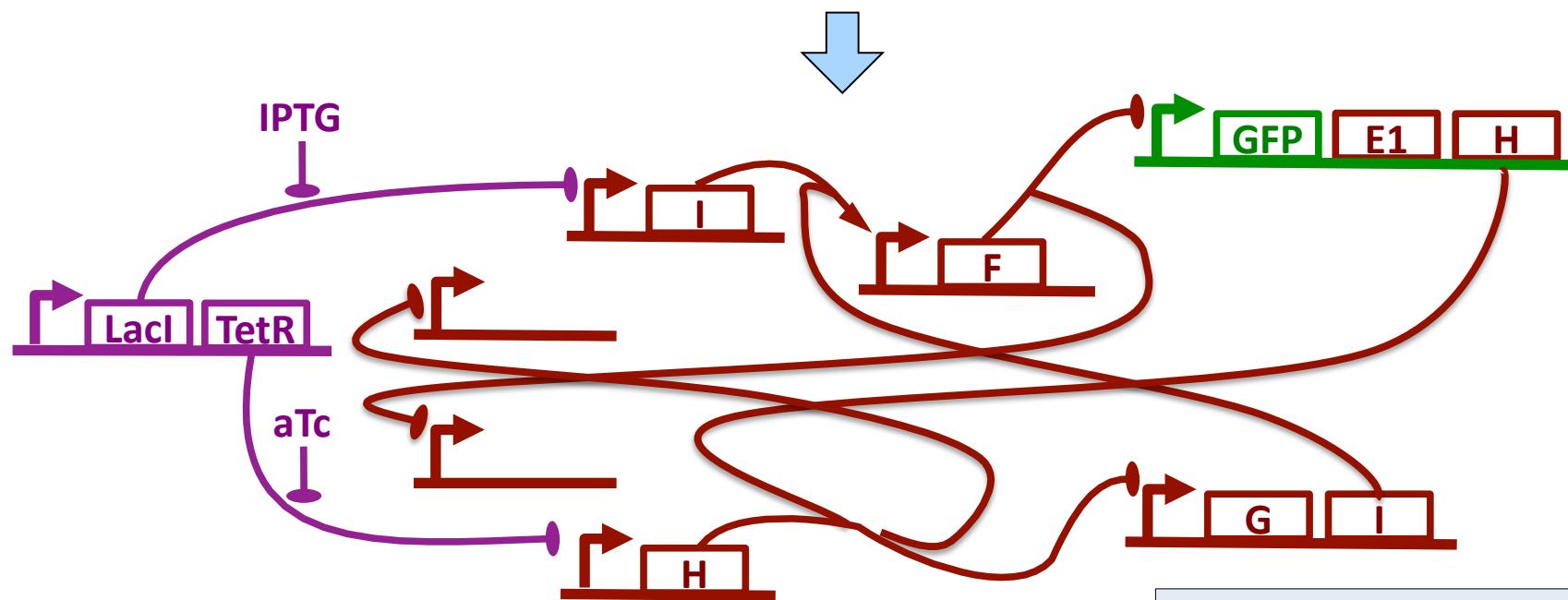
*Unoptimized: 15 functional units, 13 transcription factors*

*Copy Propagation*<sub>51</sub>

# Optimization of Complex Designs

```
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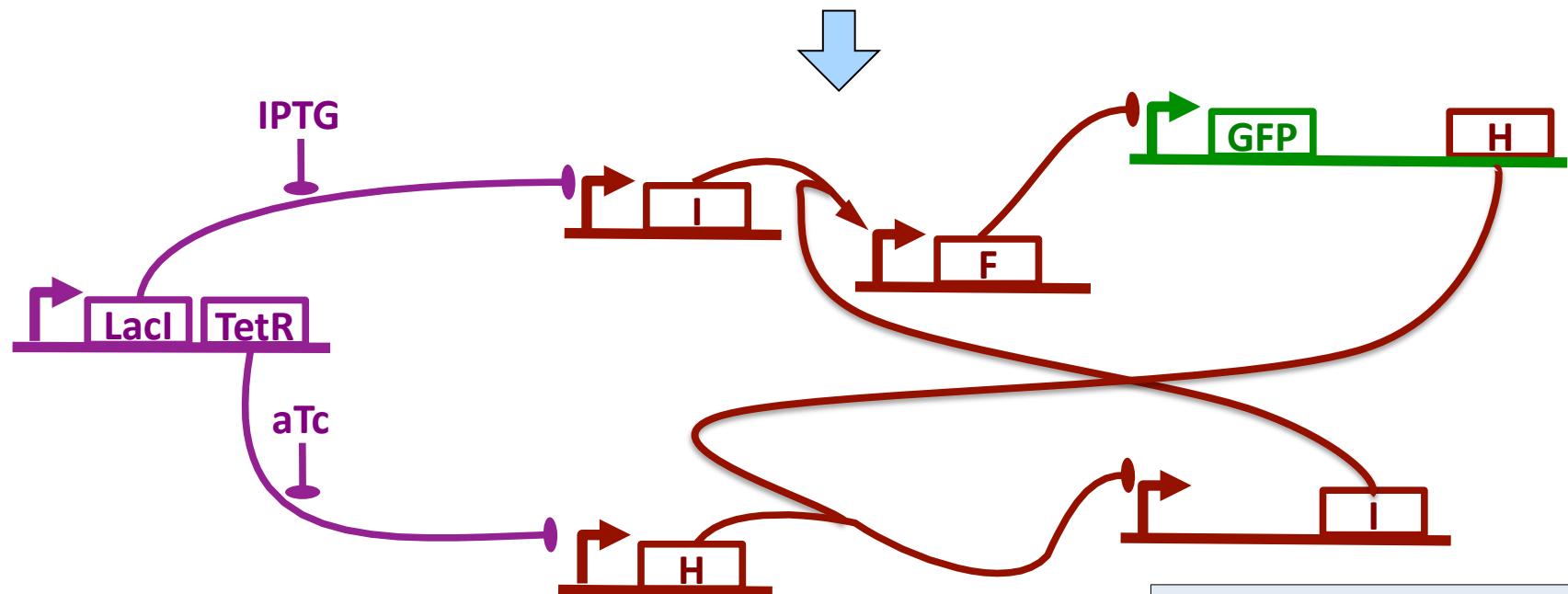
*Unoptimized: 15 functional units, 13 transcription factors*

*Common Subexp. Elim.*

# Optimization of Complex Designs

```
(def sr-latch (s r)
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```



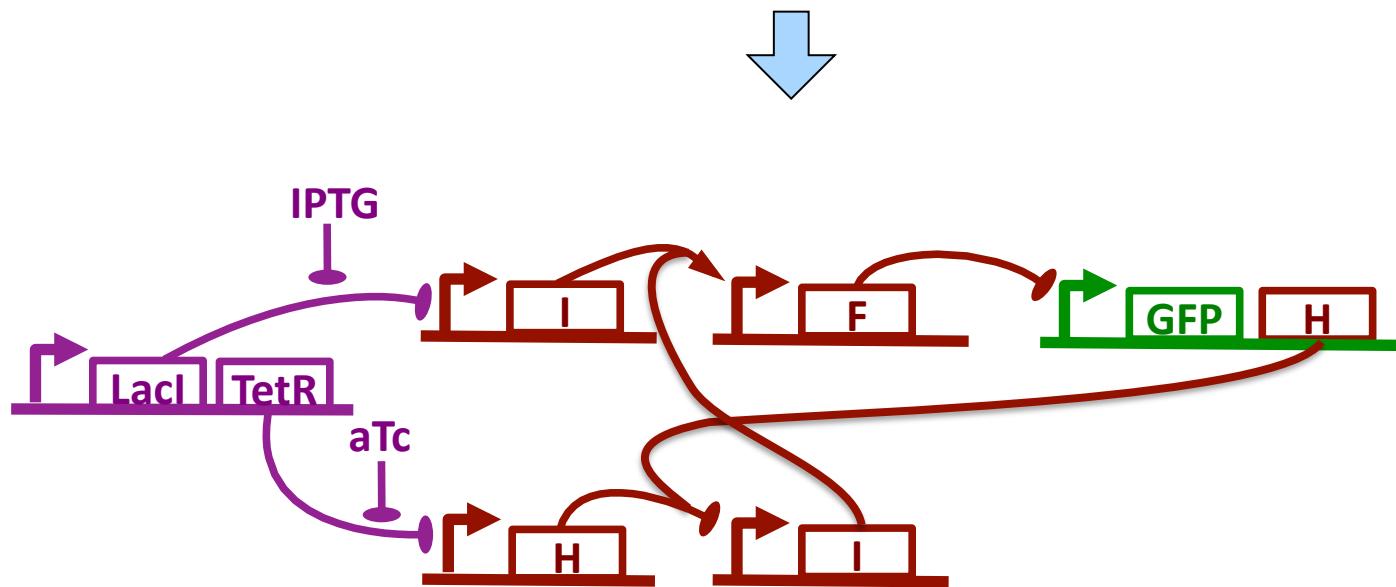
*Unoptimized: 15 functional units, 13 transcription factors*

**Dead Code Elimination** 93

# Optimization of Complex Designs

```
(def sr-latch (s r)
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    o))  

(green (sr-latch (aTc) (IPTG)))
```

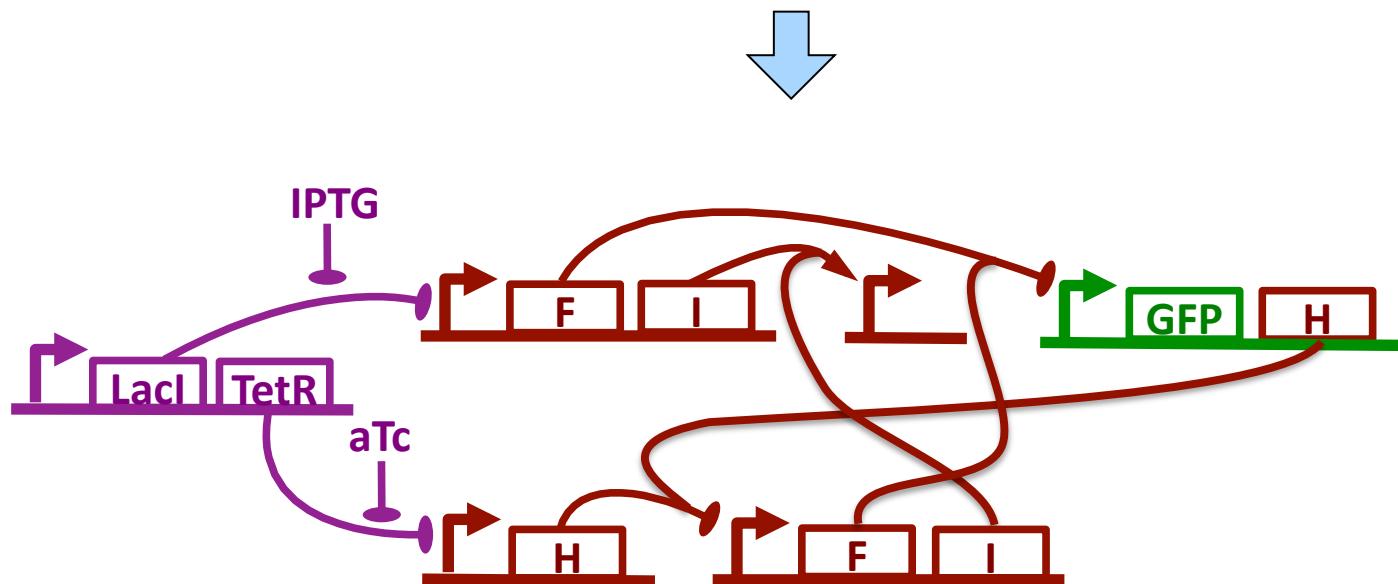


*Unoptimized: 15 functional units, 13 transcription factors*

# Optimization of Complex Designs

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(def sr-latch (s r)
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```



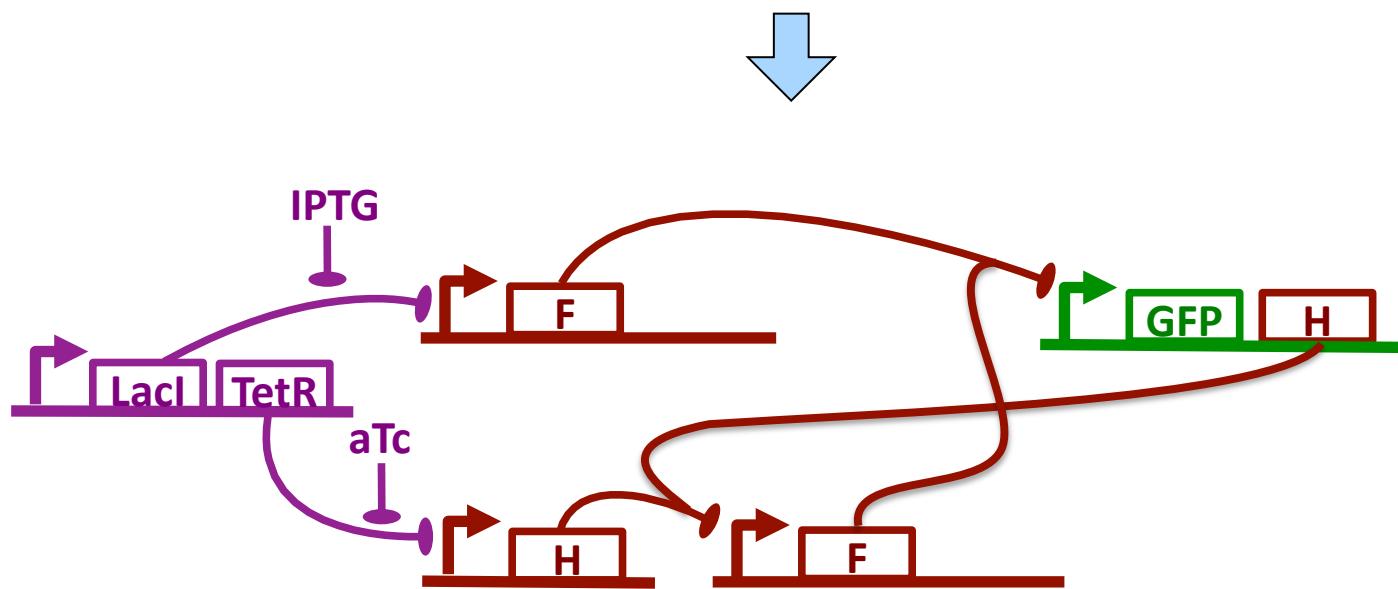
*Unoptimized: 15 functional units, 13 transcription factors*

**NOR Compression**<sub>55</sub>

# Optimization of Complex Designs

```
(def sr-latch (s r)
  (letfed+ ((o boolean (not (or r o-bar)))
            (o-bar boolean (not (or s o))))
    o))  

(green (sr-latch (aTc) (IPTG)))
```



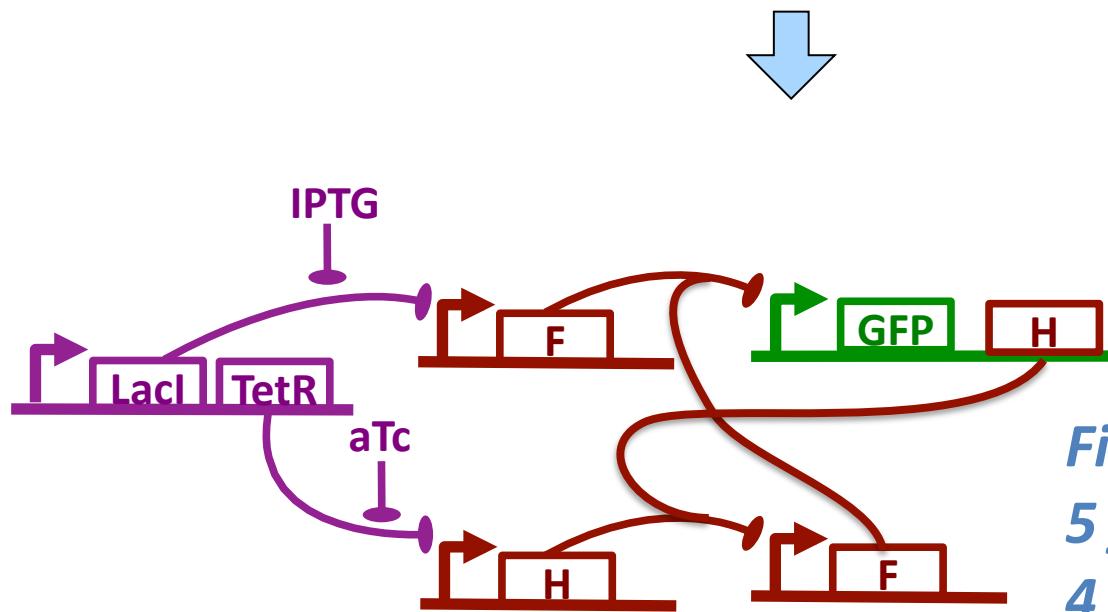
*Unoptimized: 15 functional units, 13 transcription factors*

**Dead Code Elimination** 90

# Optimization of Complex Designs

```
(def sr-latch (s r)
  (letfed+ ((o boolean (not (or r o-bar)))
            (o-bar boolean (not (or s o))))
    o))  

(green (sr-latch (aTc) (IPTG)))
```



*Final Optimized:*  
*5 functional units*  
*4 transcription factors*

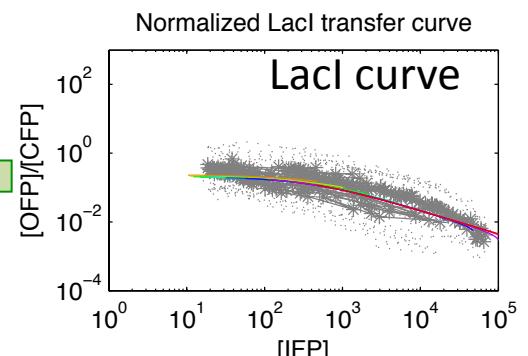
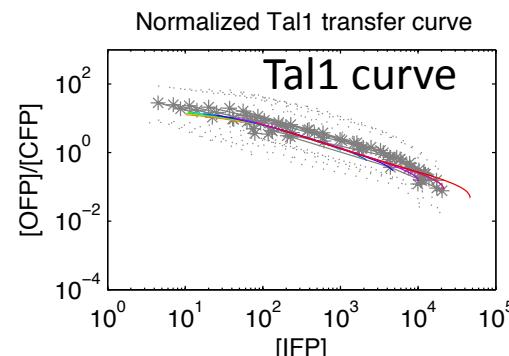
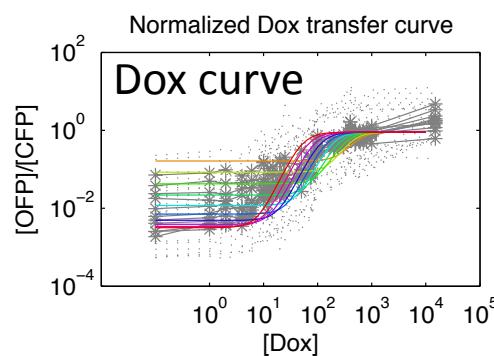
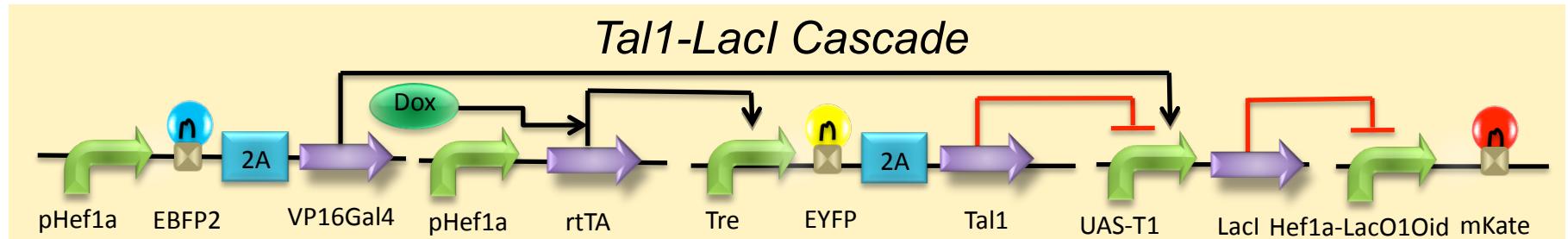
*Unoptimized: 15 functional units, 13 transcription factors*

# Compilation & Optimization Results:

---

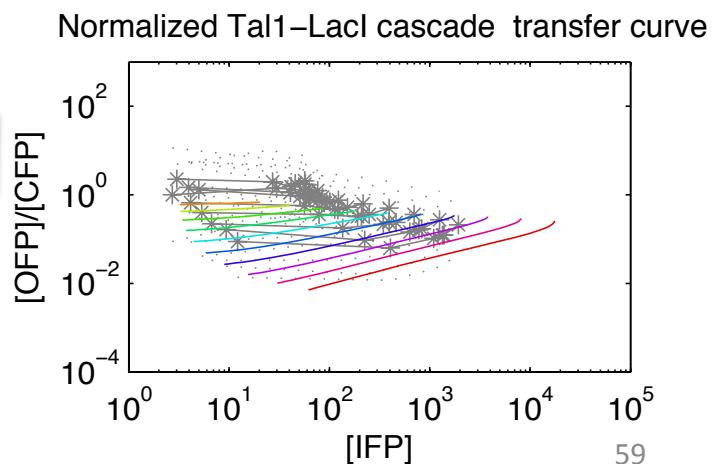
- Automated GRN design for arbitrary boolean logic and feedback systems
  - Verification in ODE simulation
- Optimization competitive with human experts:
  - Test systems have 25% to 71% complexity reduction
  - Optimized systems are often homologous with hand designed networks

# Realization with Characterized DNA parts

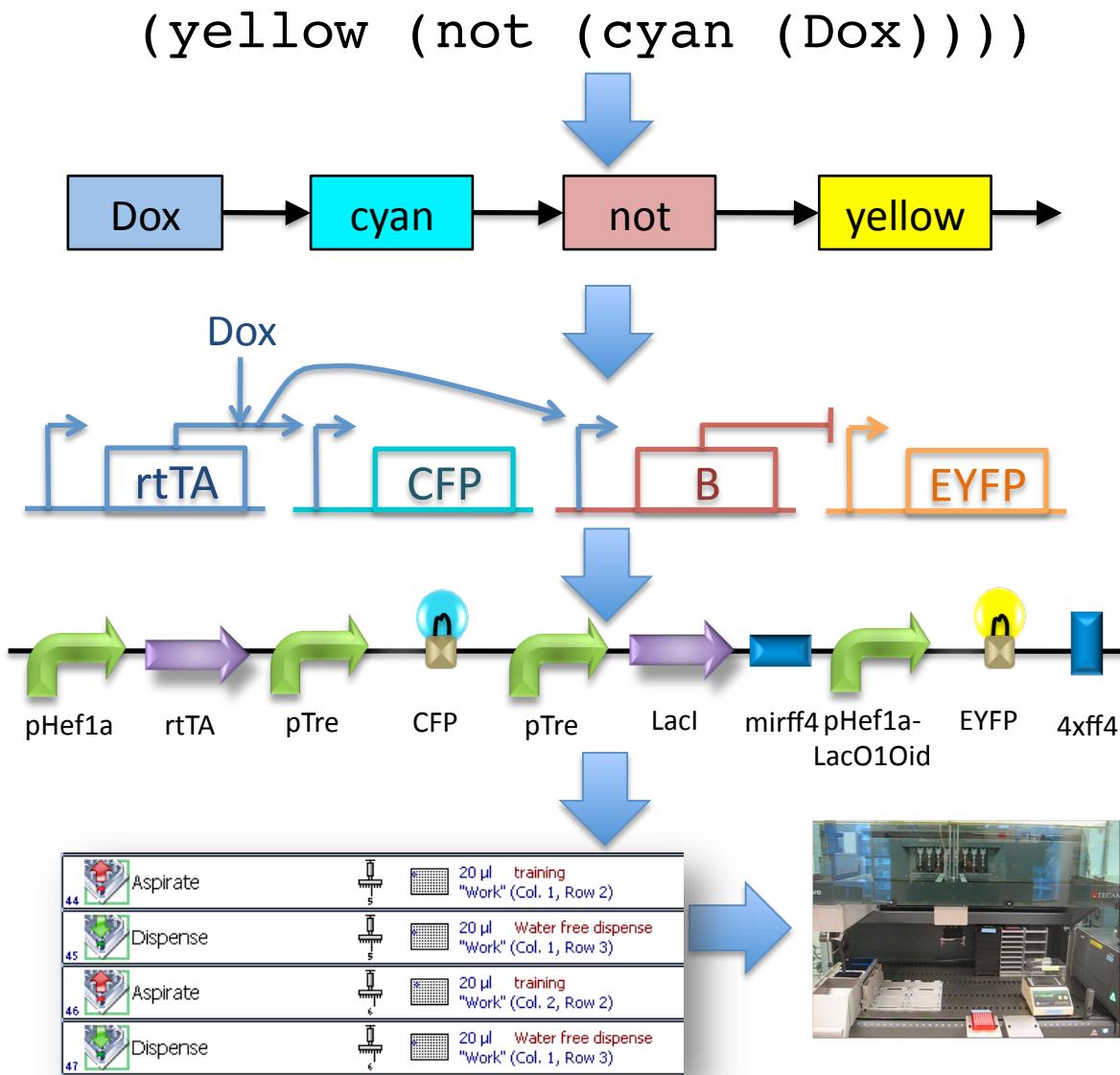


- Model → Experiment:
  - Low copy: no effect → no effect
  - High copy: 30x → 10x
  - Gradual transition → gradual transition
  - Max ~ $10^0$  → 3x higher – 2A effect?

Predict

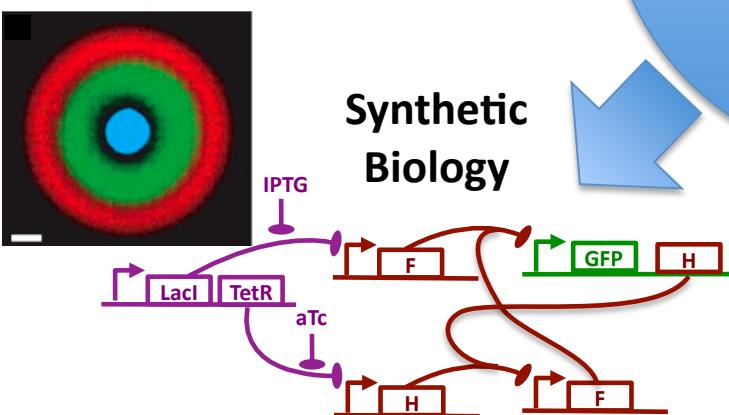
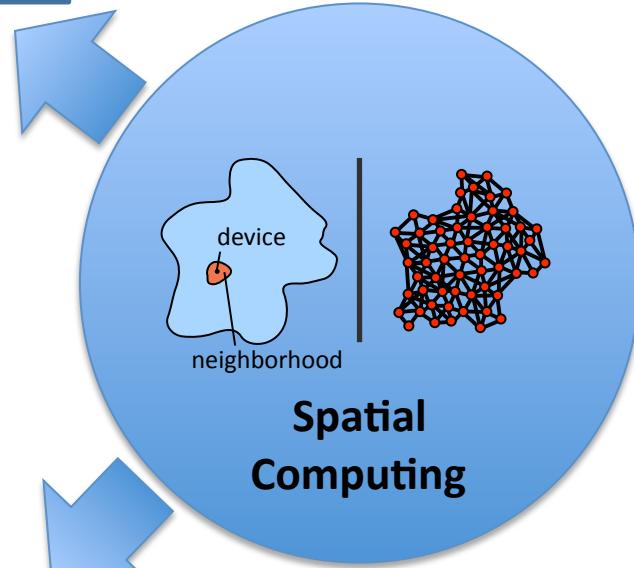


# Onward Through the Tool-Chain...



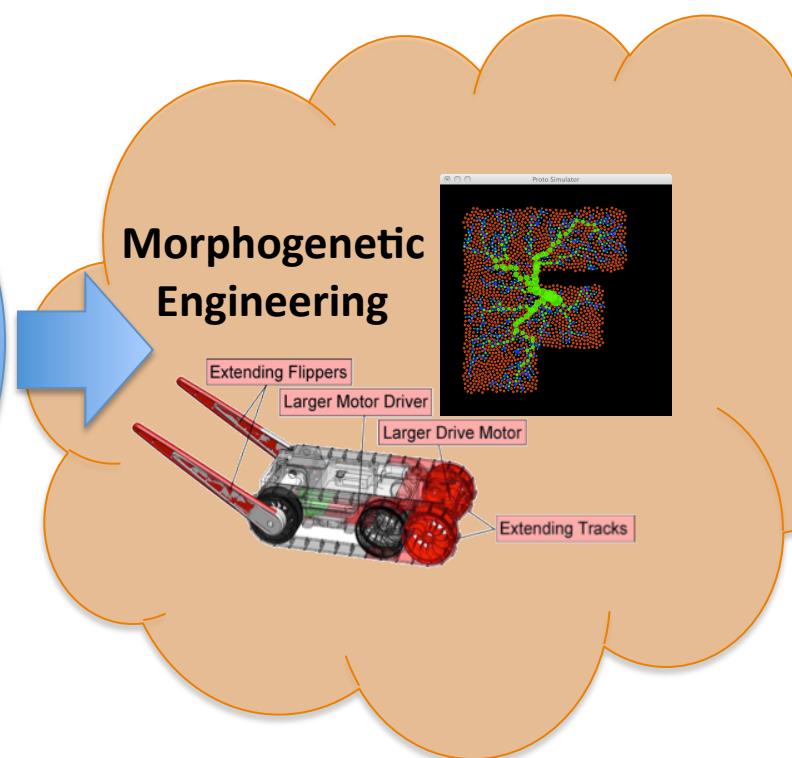


## Distributed Power Demand Response

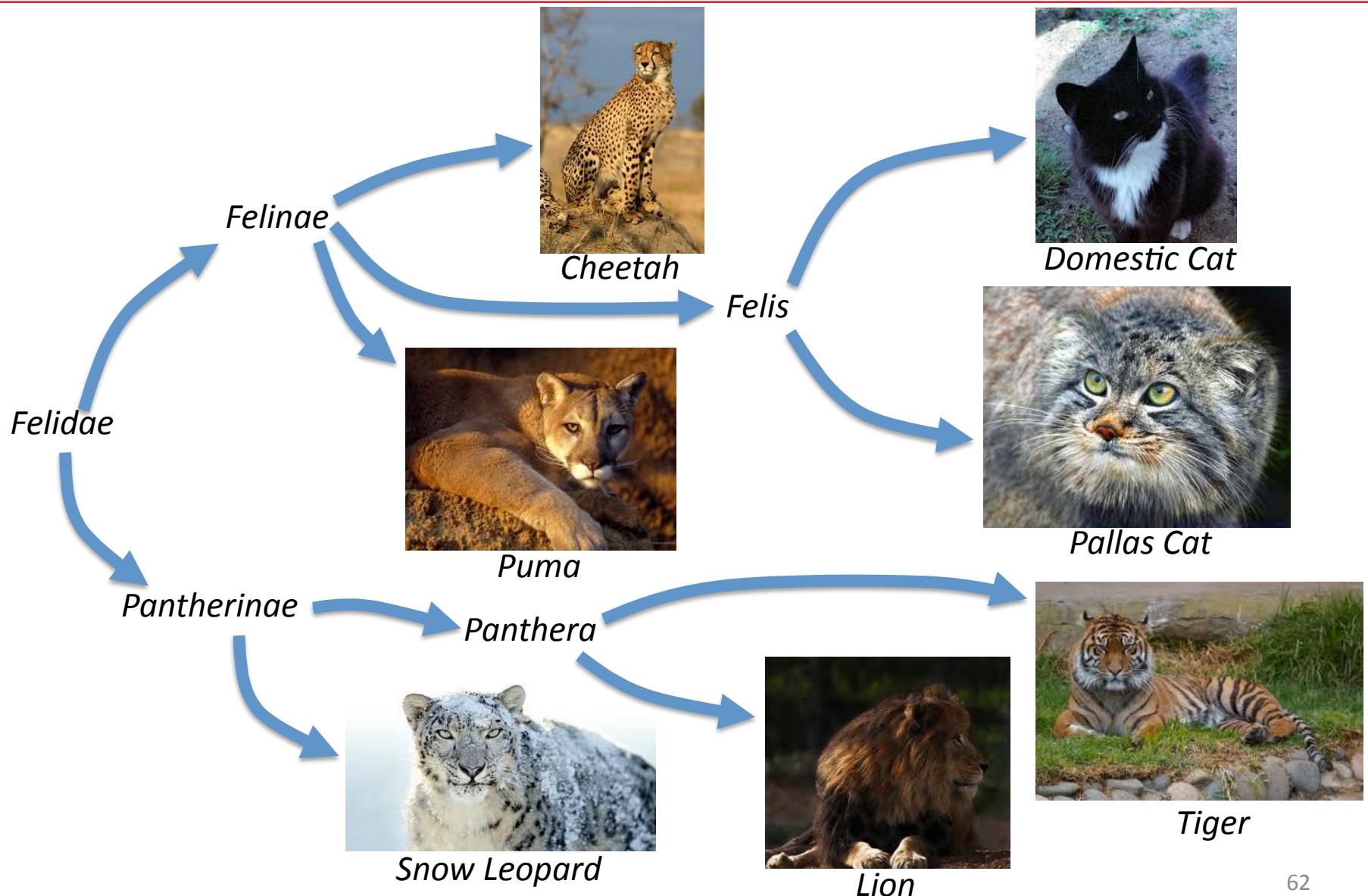


## Synthetic Biology

*How can the parts of a design work together to adapt it to new uses?*



# Morphogenesis enables natural variation



# A phylogeny of engineered systems?



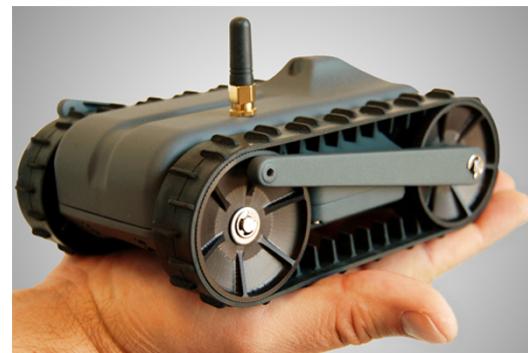
*PackBot*



*SUGV*



*Warrior*



*LANdroid*



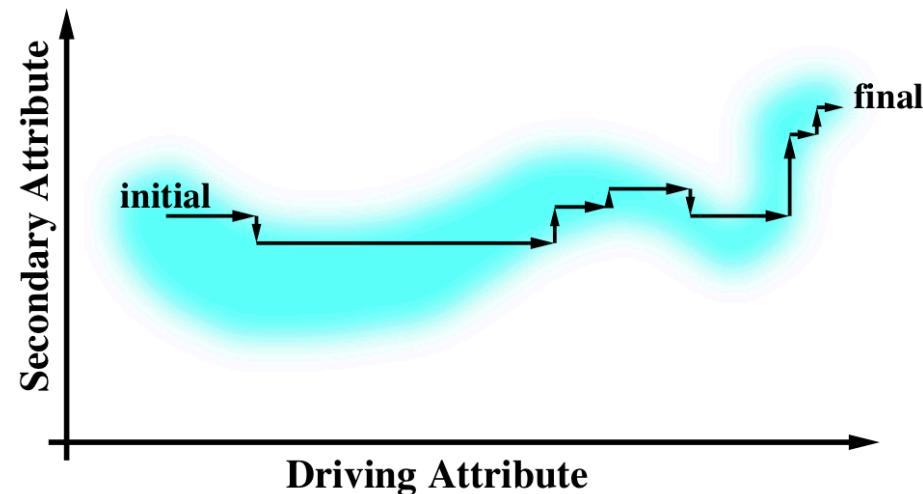
*miniDroid*

# Functional Blueprints

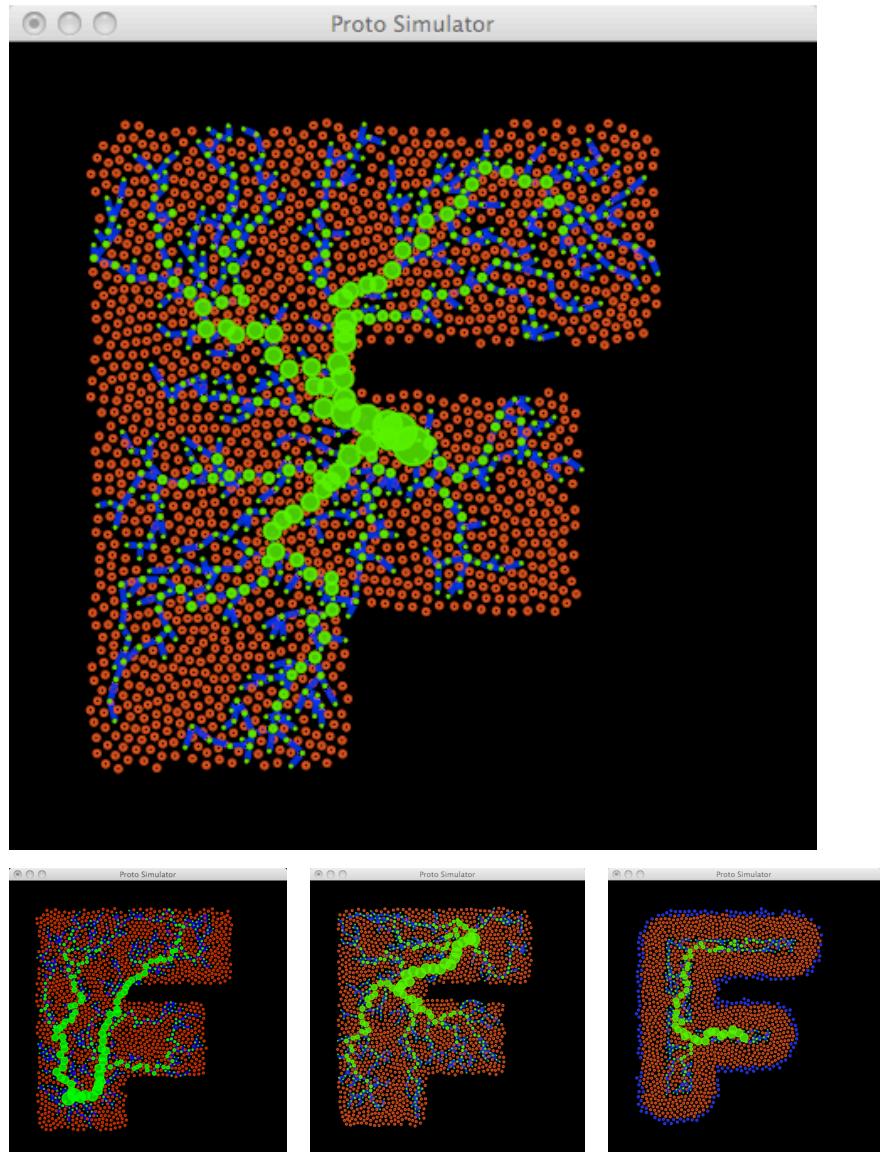
1. Functional behavior that degrades gracefully
2. Metric for degree and direction of stress
3. Incremental adjustment program for stress relief
4. Initial viable system

*Idea: incremental motion in viable design space*

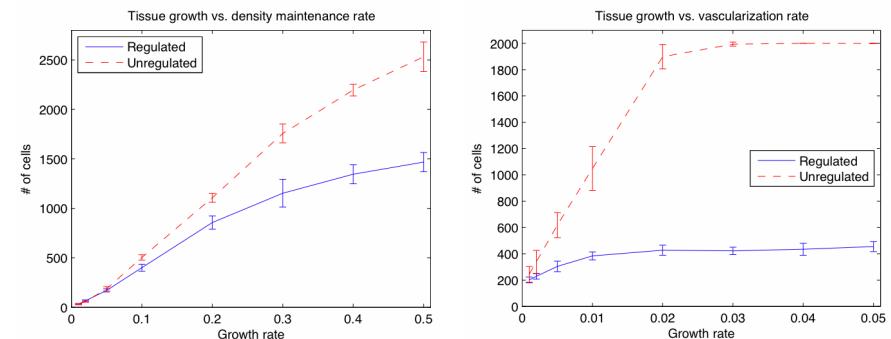
*Abstract functional blueprint networks converge reliably and >100x faster than GAs*



# Example: “Cartoon” Vascularization



- Functional blueprint model of vascularization
  - Stress: oxygen, elastic stress
  - Adjustment: leaking, vessel grow/shrink
- Red cells are healthy, blue cells are oxygen-deficient
- Can model vasculatization and density co-regulation



# What if your robot can climb stairs...

---



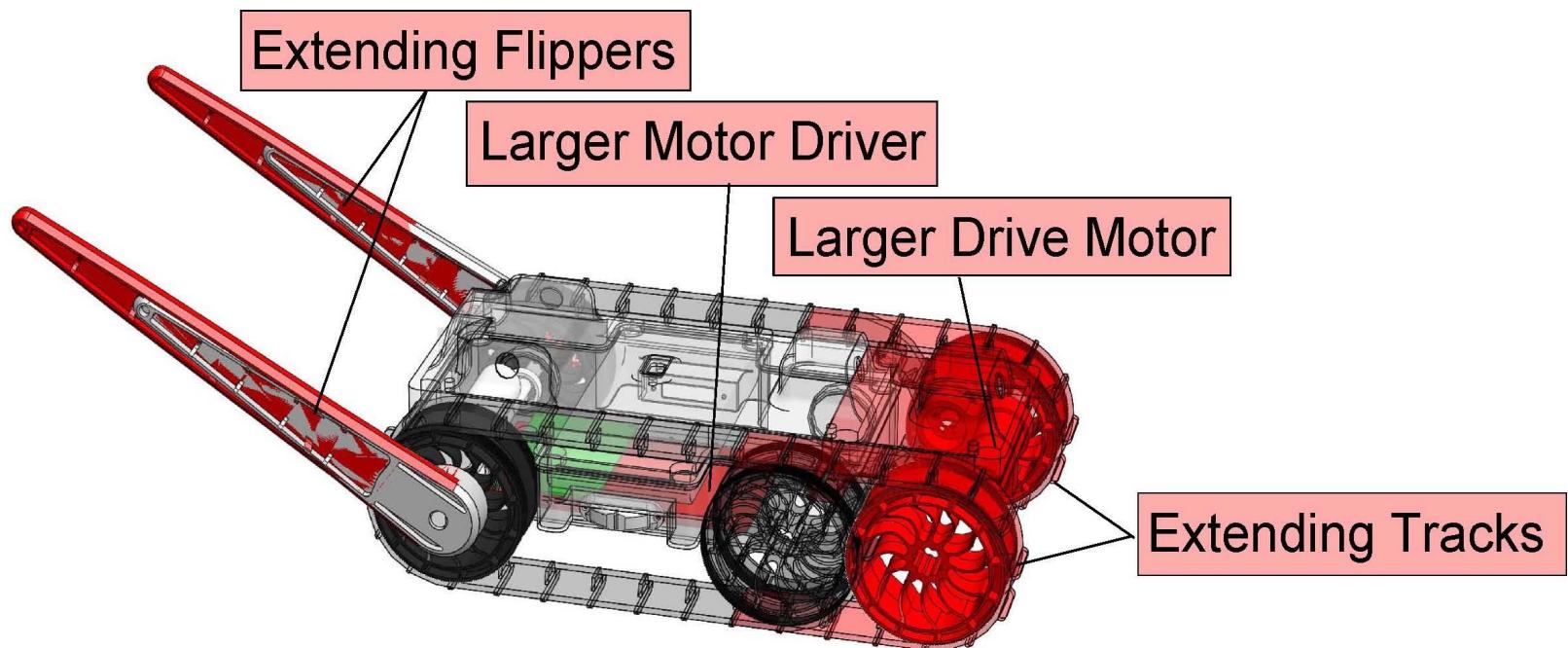
... but you want to check cars for IEDs?

**Raytheon**  
BBN Technologies



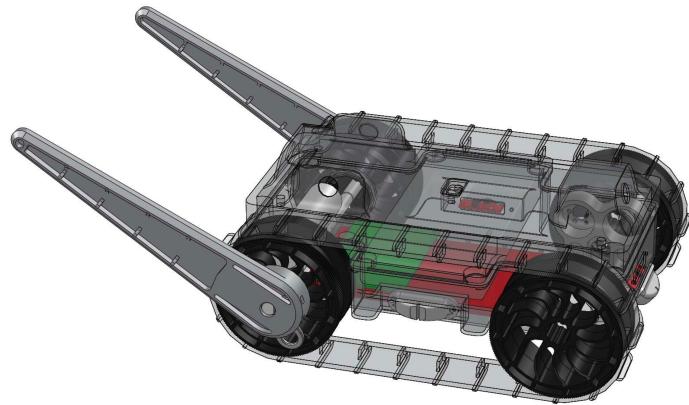
# Problem: Redesign Complexity

Even “simple” robots require careful design of many interacting components...



... and small changes have large consequences.

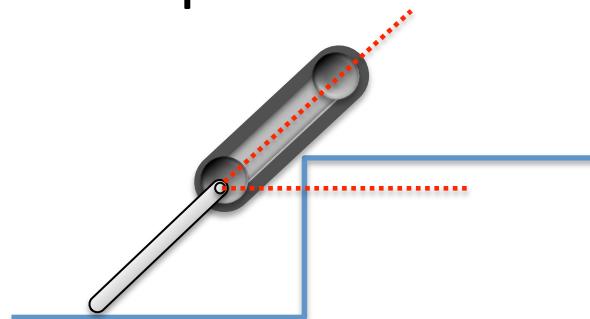
# iRobot miniDroid Functional Blueprints



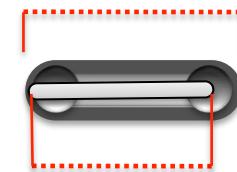
Functional blueprints requirements:

- Behavior that degrades gracefully
- Metric for stress degree & direction
- Incremental adjustment program
- Initial viable design

Examples:



Step Climbing  
(via ascent angle)

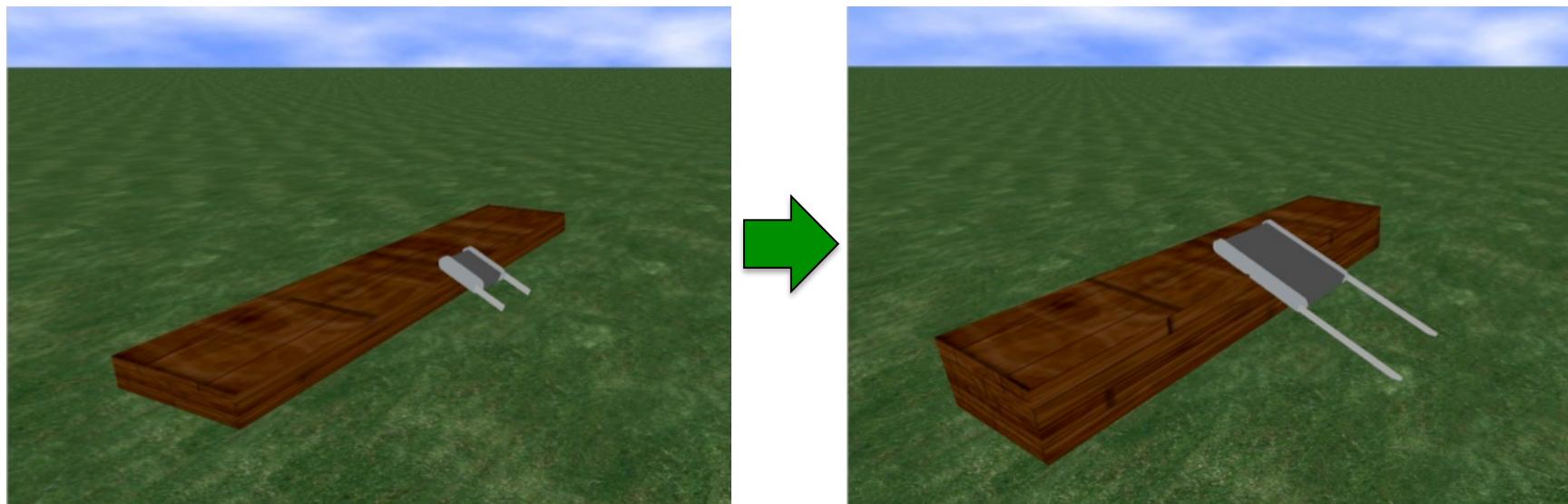


Flipper/Body Ratio



Self-Righting  
(via torque/mass)

# 5x Variation Driven by Step Height

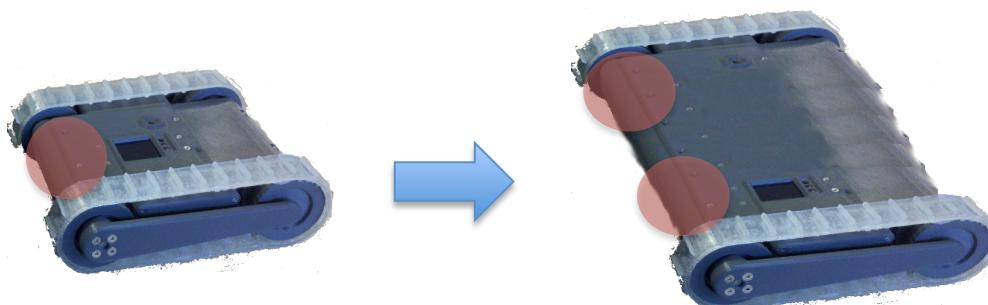


# Adjusting Component Layout

- Functional blueprints control key attributes
  - The majority of design parameters are implicit!
- How are components modified and placed?

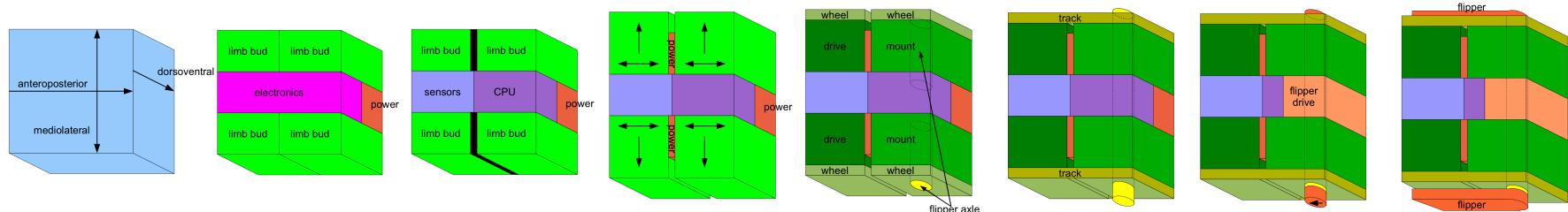


- e.g., Which way does the flipper extend? Where does the CPU go inside the robot body?
- What about changes to number or topology?



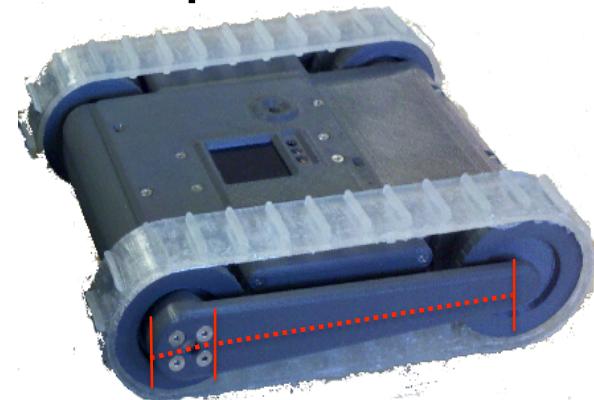
# Morphogenesis resolves design constraints

Manifold evolution based on biological development



Implicit parameters specified through geometric relationships developed between components

- Abstraction of components
- Reduced dimensionality
- Greater design flexibility



Flipper Length = Axe + Extension

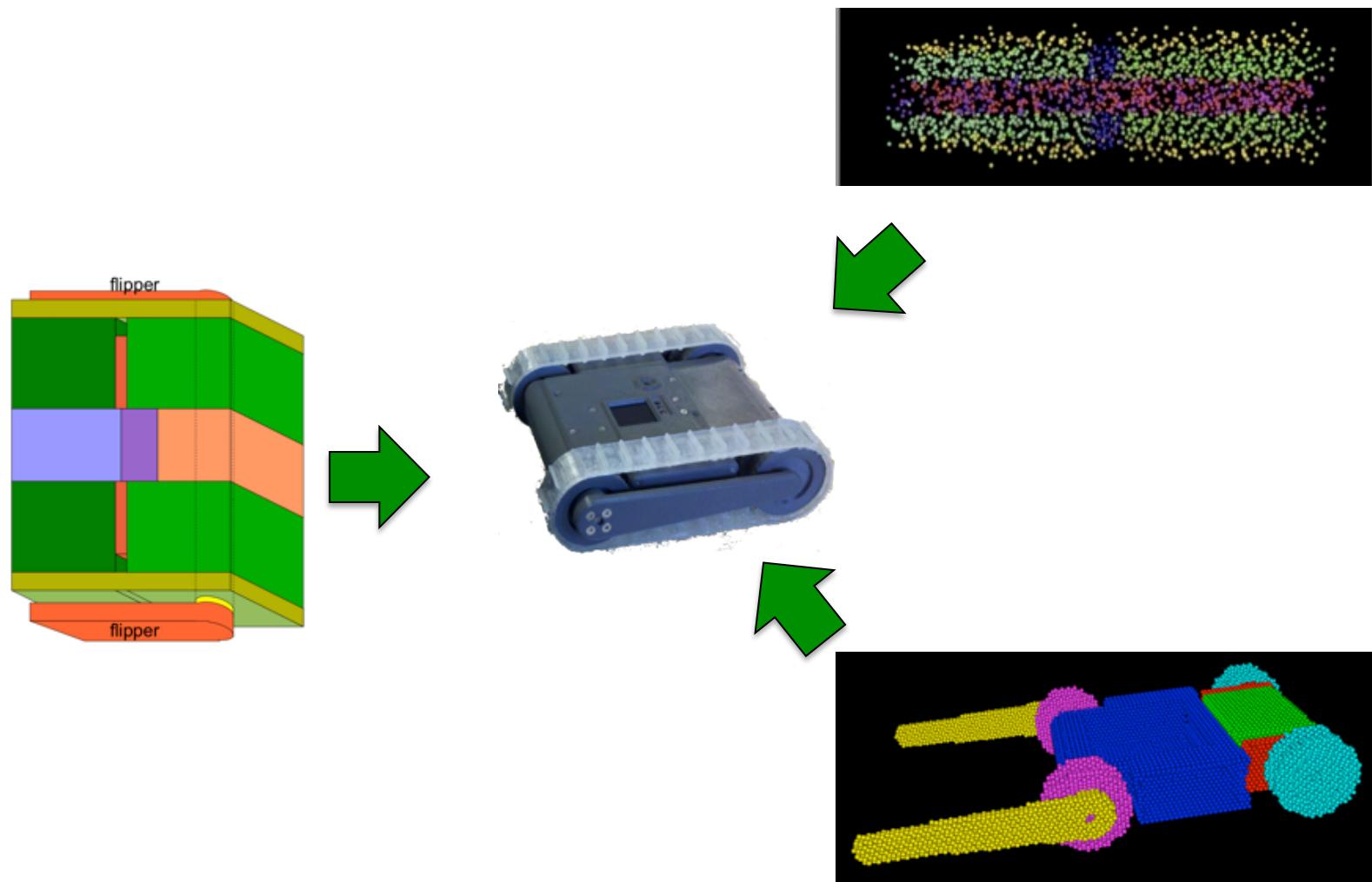
# Developmental Programs

---

Three levels of detail:

- Tissue-level rule definition and evaluation
- Proto cellular models of program plasticity
  - Concurrent & blended execution of rules
  - Manifold operators distort to match the structure of the space on which they execute
- Soft-body physics for tissue interaction
  - Adhesion lets components maintain spatial relations
  - Plasticity lets components “push” around and through each other

# Next Step: Model Integration



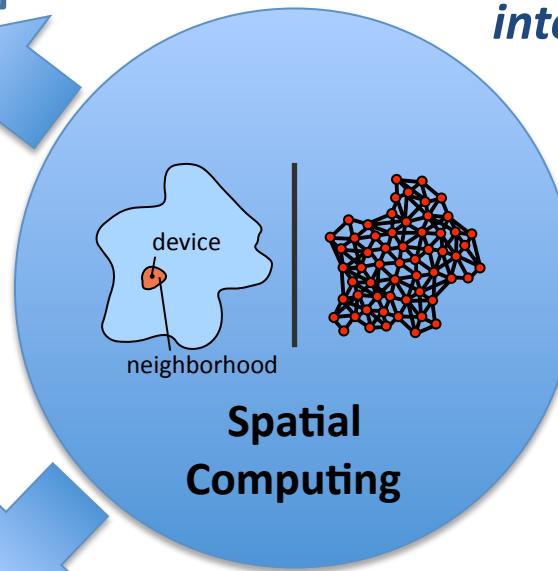
# Summary



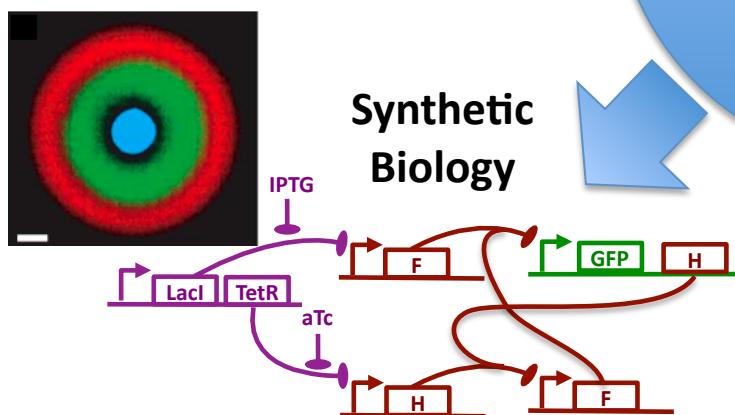
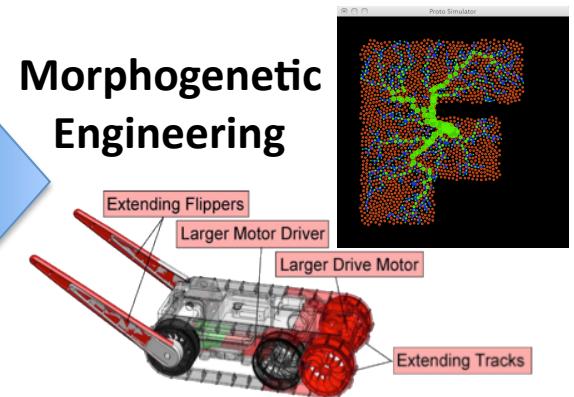
Distributed Power Demand Response

*The Amorphous Medium abstraction uses manifolds to simplify programming of scalable, robust behavior on space-filling networks*

*Proto's four families of space/time operations let geometric aggregate descriptions compile into approximating local actions*



Morphogenetic Engineering



Synthetic Biology

*Spatial abstractions can help us solve complex problems, from networks to biology and beyond...*

# Proto is available

<http://proto.bbn.com/>  
*(or google “MIT Proto”)*

- Includes libraries, compiler, kernel, simulator, platforms
- Licensed under GPL with linking exception

# Acknowledgements:

---

**Raytheon**  
**BBN Technologies**

Aaron Adler (co-PI)  
Brett Benyo  
Jeff Berliner  
Jeff Cleveland  
Jessica Lowell  
Gretchen Markiewicz  
Hala Mostafa  
Rick Schantz  
Kyle Usbeck  
Fusun Yaman  
Susan Katz, Joseph Loyall (PMs)

Interns:  
Katie McGuire, Taylor Campbell



Ron Weiss (co-PI)  
Jonathan Babb  
Noah Davidsohn  
Tim Shepard  
Nelson Elhage

**ZOME**  
ENERGY NETWORKS

Vinayak Ranade

**BOSTON**  
UNIVERSITY

Douglas Densmore (co-PI)  
Swapnil Bhatia  
Traci Haddock  
Viktor Vasilev  
Chenkai Liu

**iRobot**<sup>®</sup>

Annan Mozeika  
Ben Axelrod

**Sponsors:**



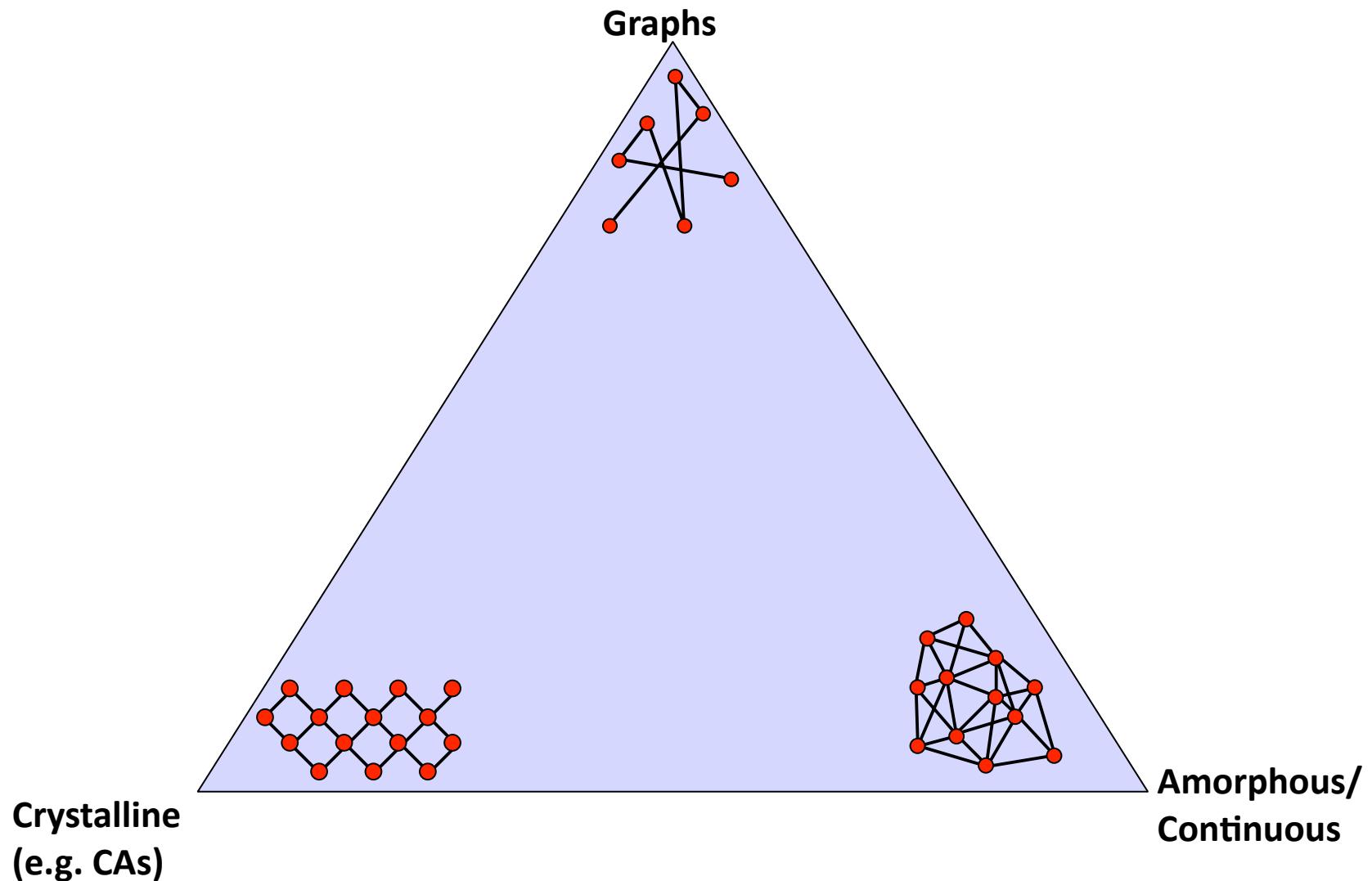
# Backup Slides: Spatial Computing

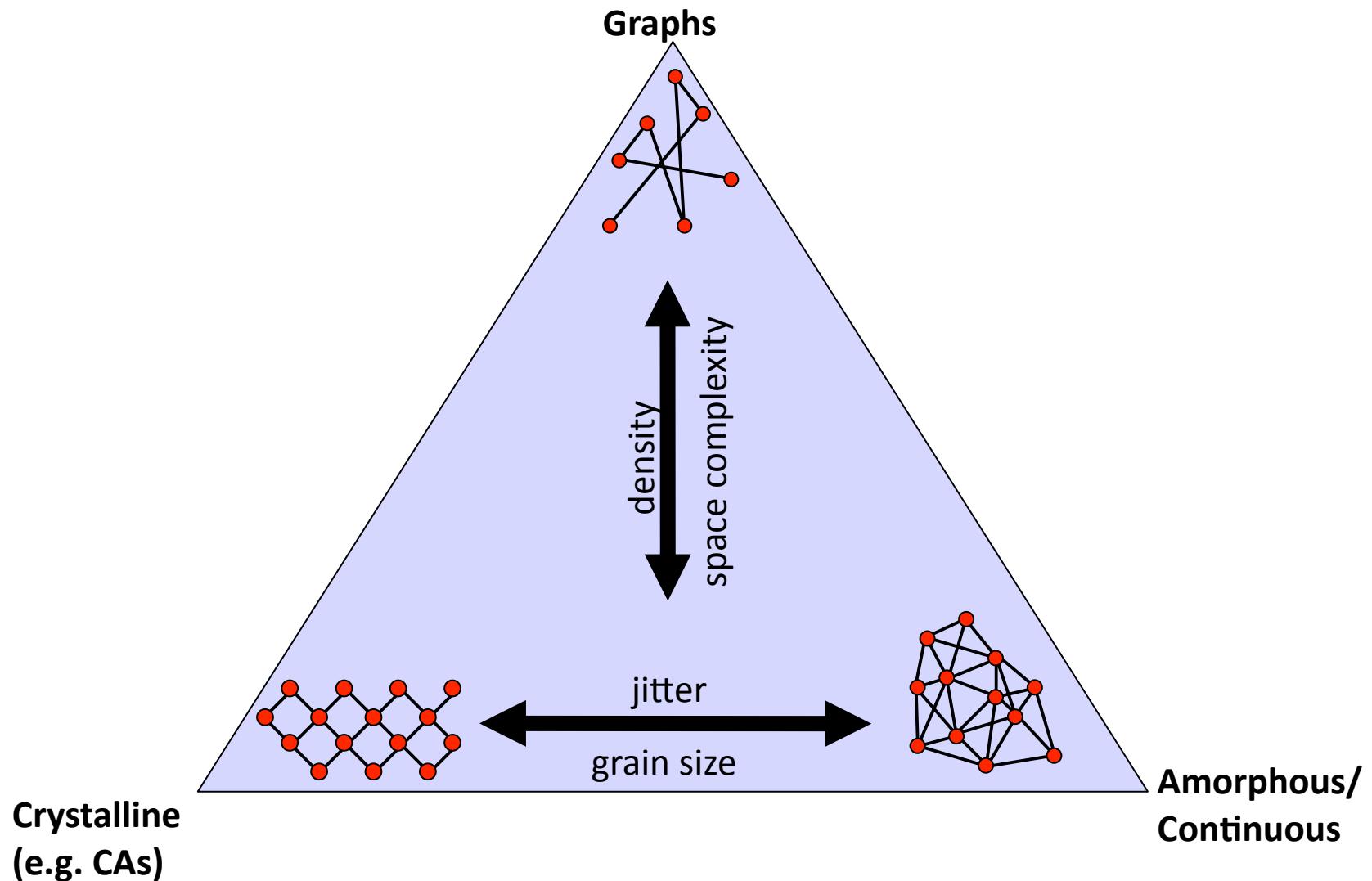
## More formally...

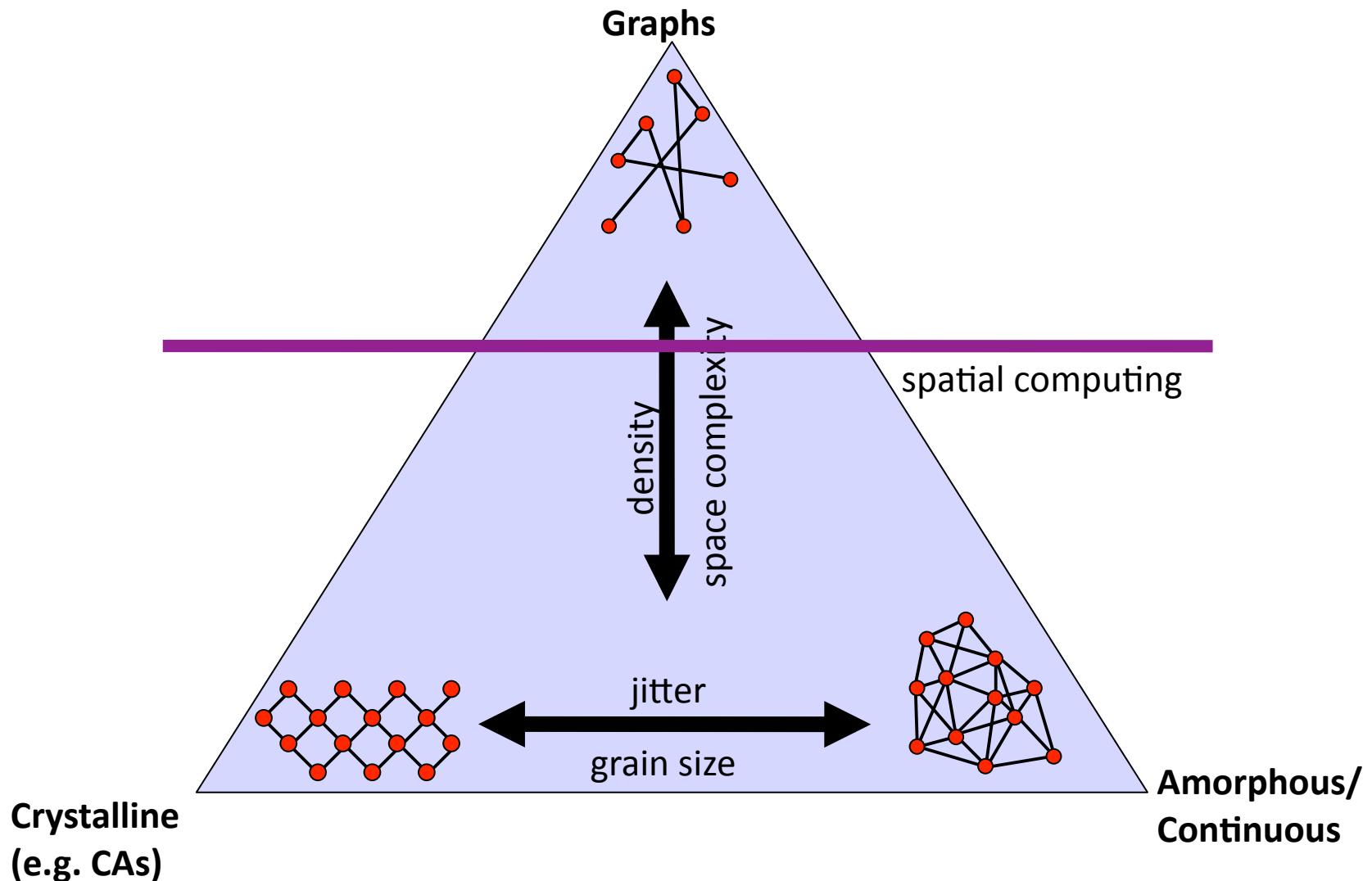
---

- A spatial computer is a collection of computational devices **distributed through** a physical space in which:
  - the difficulty of moving information between any two devices is **strongly dependent** on the distance between them, and
  - the “functional goals” of the system are **generally defined** in terms of the system's spatial structure

*Notice the ambiguities in the definition*







# Backup Slides: Demand Response

# Initial ColorPower Prototype Devices

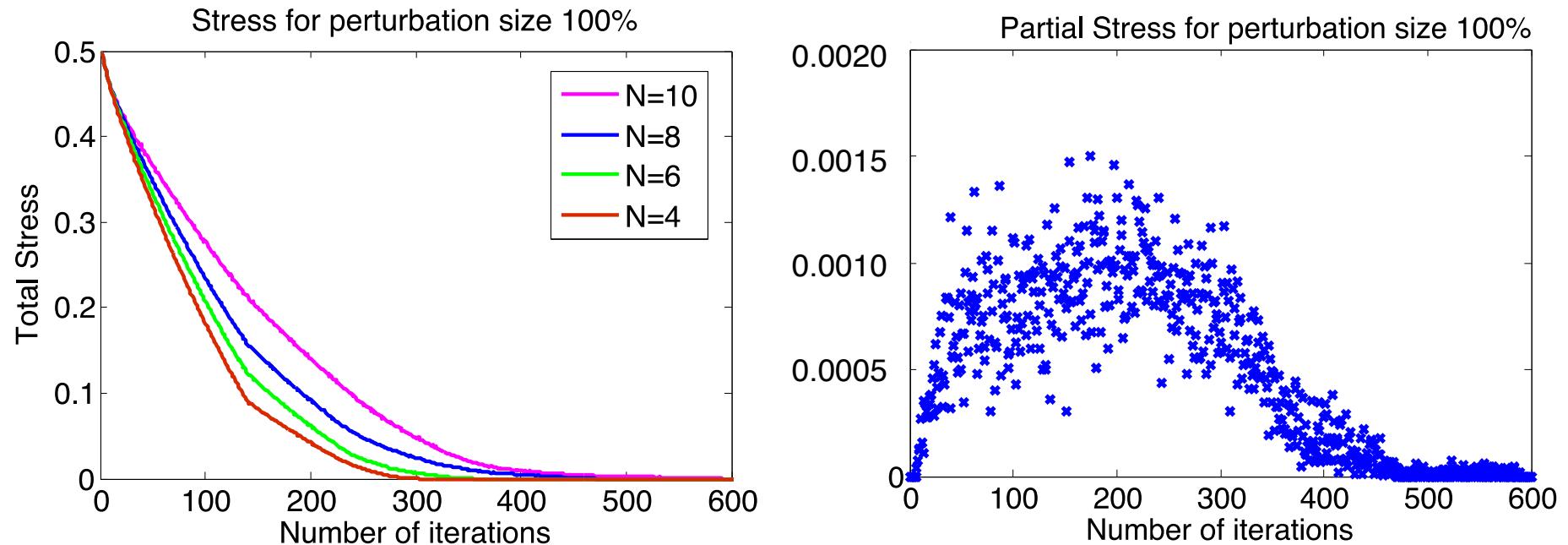
- Atmel AVR Raven
  - 8-bit processor
  - 802.15.4 wireless
- Current sensor
- Power control w. relay
- Button, rotary knob
- BOM: < \$100



# Backup Slides: Synthetic Biology

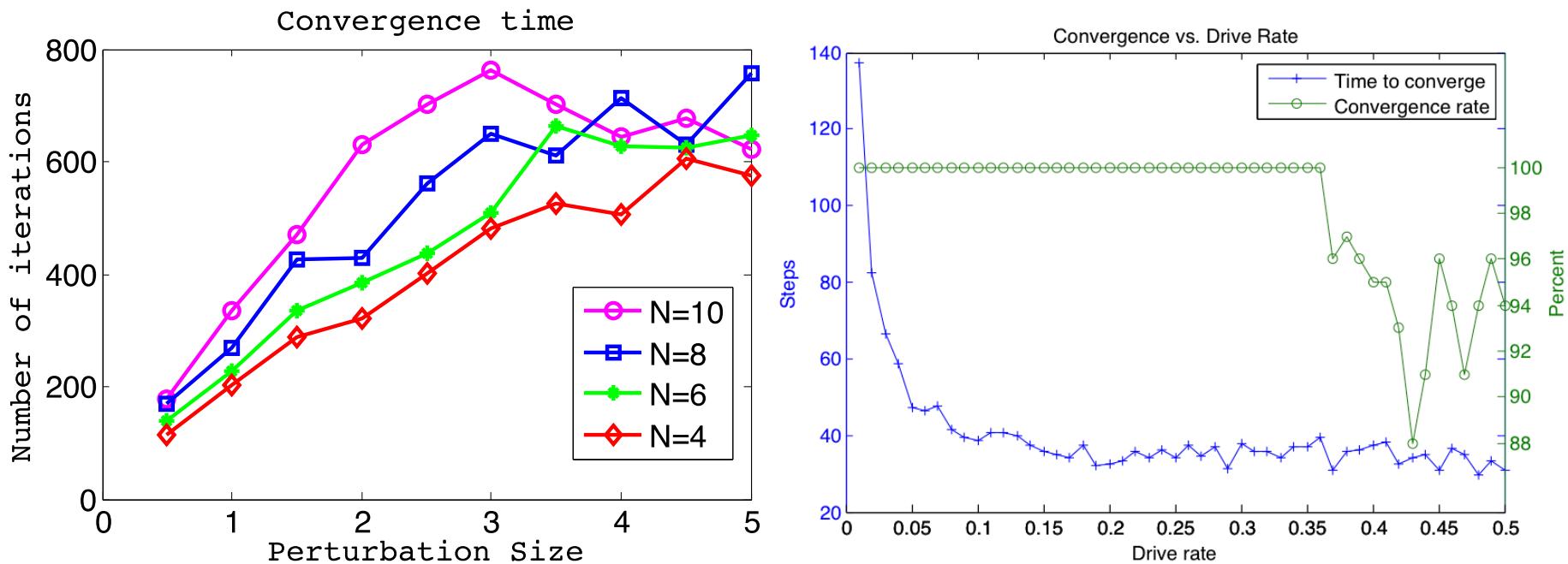
# Backup Slides: Morphogenetic Engineering

# FB Network Convergence Dynamics



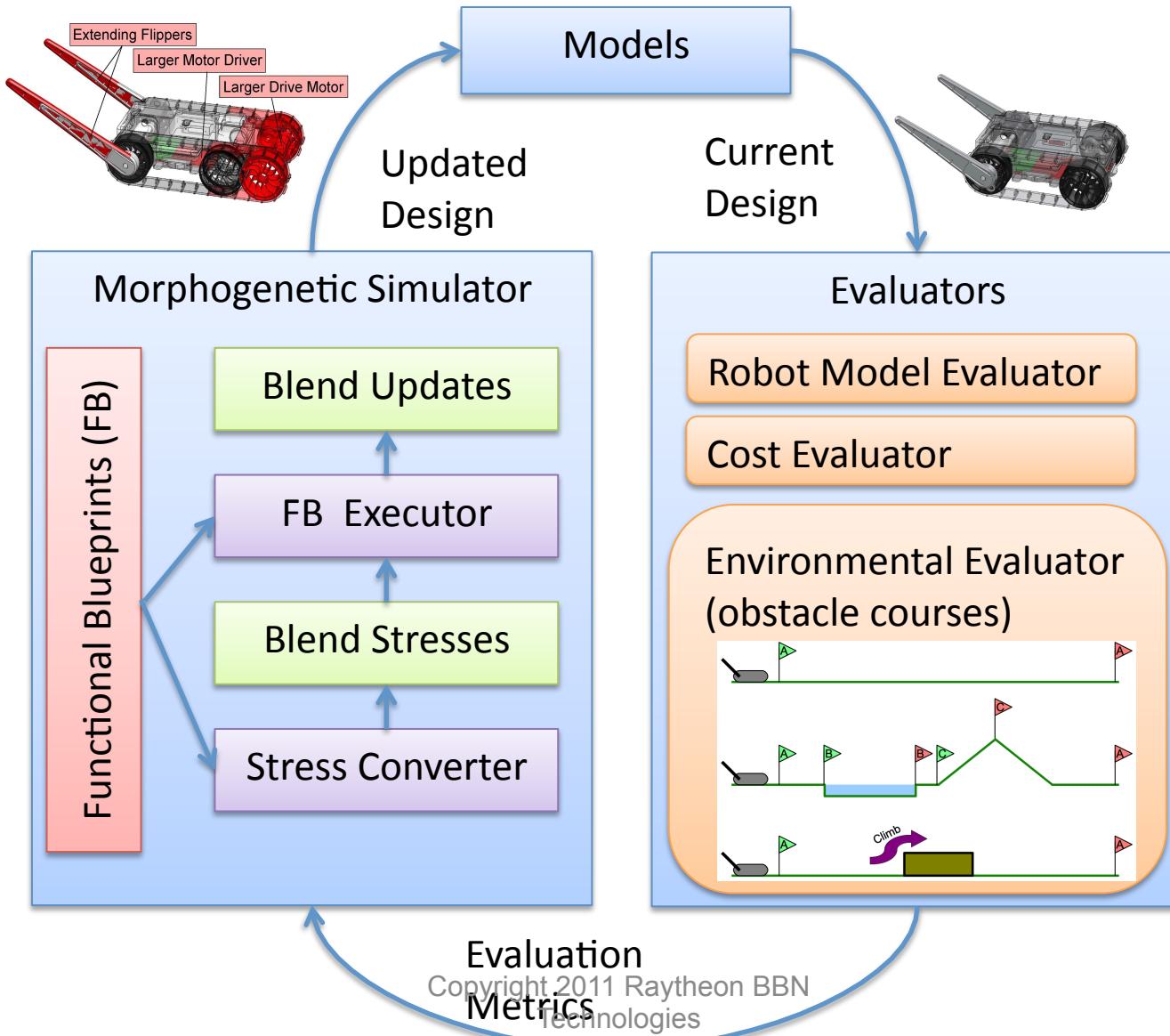
- **Experiment 1:** Induce a 100% perturbation in one of the attributes
  - For all random graphs, total stress decreases exponentially
  - Majority of the stress is the user perturbation (LEFT)
  - The rest of the system disperses the stress efficiently (RIGHT)

# Resilience to Parameter Change

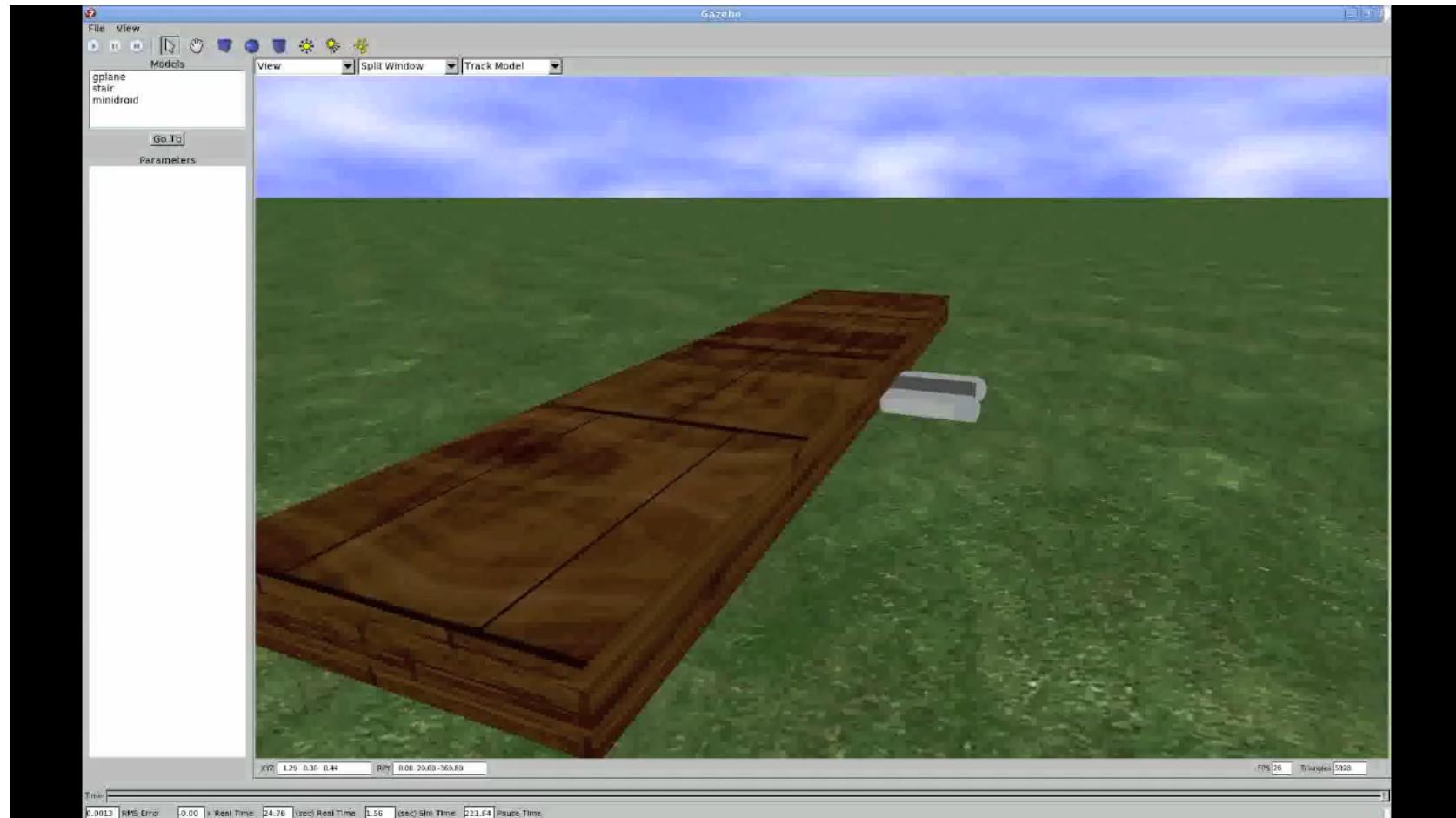


- **Experiment 2:** Vary perturbation from 100% to 500%
  - Regardless of the size of the constraint graph, linear relationship between the perturbation size and convergence time (LEFT)
- **Experiment 3:** Vary update rate (drive rate) from 0.01% to 50%
  - When increment rate is too high the system becomes non-viable (RIGHT)

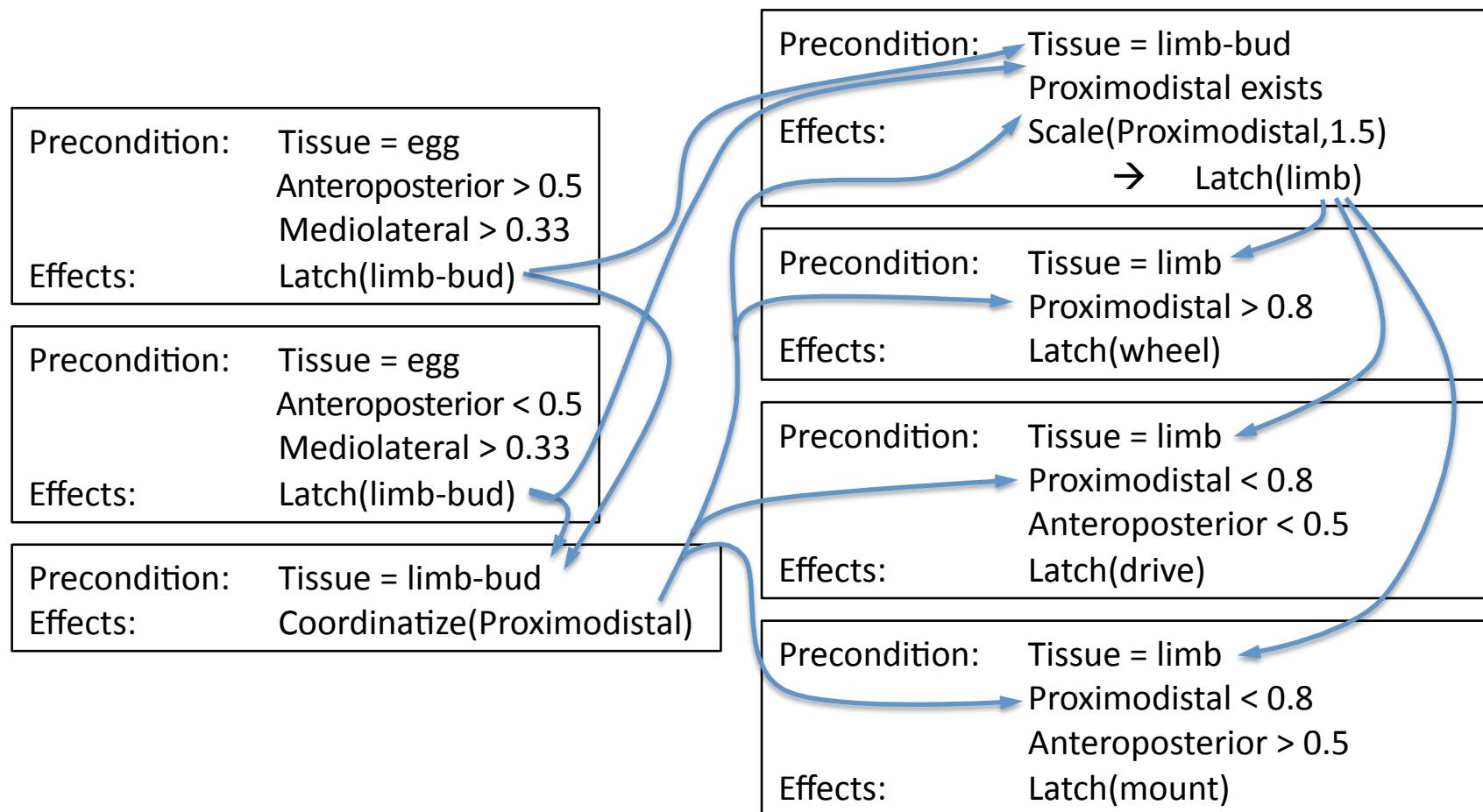
# MADV Architecture



# 5x Variation Driven by Step Height



# Program Representation: Manifold Rules



- Parallel application, continuous manifold evolution, conflict resolution by actuator blending
- Benefits: implicit relations, easy to modify/insert

# Tissue-Level Developmental Model

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# Distortable Development in Proto

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# Soft Body Tissue Development

---



# Jake's internal notes to self

# Slide Count Distribution

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- Infrastructure: 10 (title, 2 splash, 4 TOC, 3 finale)
- Spatial Computing: 7
- Proto/Amorphous Medium: 8
- Demand Response: 10
- Synthetic Biology: 17 (16 + 13 compile example)
- Morphogenetic Engineering: 11 (9+2x2 build)
- Total: 53 + infrastructure